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Specification

Edexcel GCSE in Mathematics B (2MB01) For first certification 2014

Issue 3

PEARSON

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Introduction

The Edexcel GCSE in Mathematics B is designed for use in school and colleges. It is part of a suite of GCSE qualifications offered by Edexcel. In this specification the subject content is split into three units.

The three units are:

- Unit 1, which focuses on statistics and probability content
- Unit 2, which focuses on number, algebra and geometry
- Unit 3, which focuses on number, algebra and geometry and builds on the content of Unit 2.

This specification has particular benefits for teachers and learners:

Advantages for the centre

- Content can be taught in discrete units with focused content areas for assessment.
- Centres can use different teachers to deliver units as the model supports different teaching and learning styles.
- Unit 1 contains all the statistics and probability found in the Key Stage 4 programme of study.
- Unit 1 may also be taught alongside material for GCSE statistics and can be used to support learning in science and geography.
- Support will be available from Edexcel through one- and two-year schemes of work.

Advantages for the student

- There is the opportunity for different areas of mathematics to be attempted at different tiers by students, enhancing motivation particularly at Foundation tier.
- There is an opportunity to retake the qualification in November.
- A lesser amount of non-calculator assessment, which suits some students who benefit from the support of calculator-based assessment.
- Results analysis allows centres to identify strengths and weaknesses of their students and take remedial action.

About this specification

- The assessment of all three units is at the end of the two-year programme of study.
- Accessible assessment for all students.
- Written to meet the needs of the Key Stage 4 Programme of Study.

Also available to support delivery:

- Itemised assessment feedback through ResultsPlus.
- Advice from subject specialists.
- Professional development support days.
- Teacher support material.
- Endorsed textbooks and online resources.

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Specification at a glance

The Edexcel GCSE in Mathematics B comprises three units:

• Units 1, 2, and 3

Unit 1 Statistics and Probability	*Unit code 1F: 5MB1F *Unit code 1H: 5MB1H			
Externally assessed				
Availability: June and November	30% of the total GCSE			
• First assessment: June 2014				
Overview of content				
1. Statistics				
2. Probability				
3. Number				
4. Algebra				
5. Geometry and Measures				
Overview of assessment				
One written paper				
Tiered papers				
 Foundation Tier grades C-G available 				
 Higher Tier grades A*-D available (E allowed) 				
1 hour 15 minutes Foundation tier				
• 1 hour 15 minutes Higher tier	• 1 hour 15 minutes Higher tier			
• 60 marks				
Calculator allowed				
Tiered papers				
 30-40% of Foundation Tier paper assesses the functional 	al elements of mathematics.			
$_{\odot}$ 20-30% of Higher Tier paper assesses the functional ele	ements of mathematics.			

*See Appendix 3 for description of this code and all other codes relevant to this qualification.

Unit 2	Number, Algebra, Geometry 1	*Unit code 2F: 5MB2F *Unit code 2H: 5MB2H
• External	y assessed	
Availabil	ty: June and November	30% of the total GCSE
First ass	essment: June 2014	
Overview of	content	
1. Number		
2. Algebra		
3. Geometry		
4. Measures		
Overview of	assessment	
One writ	ten paper	
Tiered parts	apers	
o Four	dation Tier grades C-G available	
∘ High	er Tier grades A*-D available (E allowed)	
• 1 hour 1	5 minutes Foundation tier	
• 1 hour 1	5 minutes Higher tier	
• 60 mark	5	
Non-calc	ulator	
Tiered parts	apers	
o 30-4	0% of Foundation Tier paper assesses the functional elements of	of mathematics.
o 20-3	0% of Higher Tier paper assesses the functional elements of ma	athematics.

*See Appendix 3 for description of this code and all other codes relevant to this qualification

Unit 3 Number, Algebra, Geometry 2	*Unit code 3F: 5MB3F *Unit code 3H: 5MB3H
Externally assessed	
Availability: June and November	40% of the total GCSE
First assessment: June 2014	
Overview of content	
1. Number	
2. Algebra	
3. Geometry	
4. Measures	
Overview of assessment	
One written paper	
Tiered papers	
 Foundation Tier grades C-G available 	
\circ Higher Tier grades A*-D available (E allowed)	
1 hour 30 minutes Foundation tier	
• 1 hour 45 minutes Higher tier	
• 80 marks	
Calculator allowed	
Tiered papers	
$_{\odot}$ 30-40% of Foundation Tier paper assesses the functional elem	ients of mathematics.
$_{\odot}$ 20-30% of Higher Tier paper assesses the functional elements	of mathematics.

*See Appendix 3 for description of this code and all other codes relevant to this qualification.

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National Qualifications Framework (NQF) criteria

This specification complies with the requirements of the common criteria, the GCSE qualification criteria, subject criteria for Mathematics and the Key Stage 4 Programme of Study for Mathematics, which are prescribed by the regulatory authorities.

Key subject aims

This qualification in Mathematics encourages students to develop confidence in, and have a positive attitude towards, mathematics and they recognise the importance of mathematics in their own lives and to society. This qualification prepares students to make informed decisions about the use of technology, the management of money, further learning opportunities and career choices.

Knowledge and understanding

This Edexcel GCSE in Mathematics B qualification requires students to:

- Develop knowledge, skills and understanding of mathematical methods and concepts, including:
 - Number
 - Algebra
 - Geometry
 - Measures
 - Statistics
 - Probability.
- Use their knowledge and understanding to make connections between mathematical concepts.
- Be able to apply the functional elements of mathematics to solve problems in real-life situations.

This Edexcel GCSE in Mathematics B gives students the opportunity to develop the ability to:

- acquire and use problem-solving strategies
- select and apply mathematical techniques and methods in mathematical, every day and real-world situations
- reason mathematically, make deductions and inferences and draw conclusions
- interpret and communicate mathematical information in a variety of forms appropriate to the information and context.

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Subject content

The content of the specification has been grouped into topic areas:

- Number
- Algebra
- Geometry
- Measures
- Statistics
- Probability.

The specification content consists of a reference (ref), a content descriptor and examples of concepts and skills.

Content that is Higher Tier only is indicated in **bold type**.

The content of Higher Tier subsumes the content of Foundation Tier.

Concepts and skills develop through the units, under the same content descriptor.

An overview of the content follows, showing in which units content is assessed.

The same content descriptors may appear in each unit but concepts and skills are developed through the units, so the examples in concepts and skills may be different.

Ref	Content descriptor	Unit	
Number		Foundation	Higher
Na	Add, subtract, multiply and divide any number	Unit 1, Unit 2, Unit 3	Unit 1, Unit 2, Unit 3
Nb	Order rational numbers	Unit 2	Unit 2
Nс	Use the concepts and vocabulary of factor (divisor), multiple, common factor, Highest Common Factor (HCF), Least Common Multiple (LCM), prime number and prime factor decomposition	Unit 2	Unit 2
N d	Use the terms square, positive and negative square root, cube and cube root	Unit 2	Unit 2
Ne	Use index notation for squares, cubes and powers of 10	Unit 2	Unit 2
N f	Use index laws for multiplication and division of integer, fractional and negative powers	Unit 2	Unit 2
Ng	Interpret, order and calculate with numbers written in standard index form		Unit 2, Unit 3
N h	Understand equivalent fractions, simplifying a fraction by cancelling all common factors	Unit 1, Unit 2	Unit 1, Unit 2
Ni	Add and subtract fractions	Unit 2	Unit 2
Nj	Use decimal notation and recognise that each terminating decimal is a fraction	Unit 1, Unit 2	Unit 1, Unit 2
Nk	Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals	Unit 2	Unit 2, Unit 3
NI	Understand that 'percentage' means 'number of parts per 100' and use this to compare proportions	Unit 1, Unit 2	Unit 1, Unit 2
N m	Use percentage, repeated proportional change	Unit 1, Unit 3	Unit 1, Unit 3
Νn	Understand and use direct and indirect proportion		Unit 3
Νo	Interpret fractions, decimals and percentages as operators	Unit 1, Unit 2, Unit 3	Unit 1, Unit 2, Unit 3
Νр	Use ratio notation, including reduction to its simplest form and its various links to fraction notation	Unit 1, Unit 2	Unit 1, Unit 2

Ref	Content descriptor	Unit	
Number		Foundation	Higher
Nq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of operations	Unit 1, Unit 2, Unit 3	Unit 1, Unit 2, Unit 3
Nr	Use surds and π in exact calculations		Unit 2
Ns	Calculate upper and lower bounds		Unit 3
Nt	Divide a quantity in a given ratio	Unit 1, Unit 2	Unit 1, Unit 2
Nu	Approximate to specified or appropriate degrees of accuracy including a given power of ten, number of decimal places and significant figures	Unit 1, Unit 2	Unit 1, Unit 2
Nv	Use calculators effectively and efficiently, including trigonometrical and statistical functions	Unit 1, Unit 3	Unit 1, Unit 3

Ref	Content descriptor	Unit	
Algebra		Foundation	Higher
A a	Distinguish the different roles played by letter symbols in algebra, using the correct notation	Unit 1, Unit 2	Unit 1, Unit 2
Ab	Distinguish in meaning between the words 'equation', 'formula', 'identity' and 'expression'	Unit 1, Unit 2	Unit 1, Unit 2
Ac	Manipulate algebraic expressions by collecting like terms, by multiplying a single term over a bracket, and by taking out common factors, multiplying two linear expressions, factorising quadratic expressions including the difference of two squares and simplifying rational expressions	Unit 2, Unit 3	Unit 2, Unit 3
A d	Set up and solve simple equations including simultaneous equations in two unknowns	Unit 3	Unit 3
Ae	Solve quadratic equations		Unit 3
A f	Derive a formula, substitute numbers into a formula and change the subject of a formula	Unit 2, Unit 3	Unit 2, Unit 3
Ag	Solve linear inequalities in one or two variables, and represent the solution set on a number line or on a suitable diagram	Unit 3	Unit 3
A h	Use systematic trial and improvement to find approximate solutions of equations where there is no simple analytical method of solving them	Unit 3	Unit 3
Ai	Generate terms of a sequence using term-to-term and position-to-term definitions of the sequence	Unit 2	Unit 2
Аj	Use linear expressions to describe the n^{th} term of an arithmetic sequence	Unit 2	Unit 2
A k	Use the conventions for coordinates in the plane and plot points in all four quadrants, including using geometric information	Unit 2, Unit 3	Unit 2, Unit 3
AI	Recognise and plot equations that correspond to straight-line graphs in the coordinate plane, including finding gradients	Unit 1, Unit 2	Unit 1, Unit 2, Unit 3
A m	Understand that the form $y = mx + c$ represents a straight line and that <i>m</i> is the gradient of the line and <i>c</i> is the value of the <i>y</i> -intercept		Unit 1, Unit 2
A n	Understand the gradients of parallel lines		Unit 2

Ref	Content descriptor	Unit	
Algebra		Foundation	Higher
Αο	Find the intersection points of the graphs of a linear and quadratic function, knowing that these are the approximate solutions of the corresponding simultaneous equations representing the linear and quadratic functions		Unit 3
Ар	Draw, sketch, recognise graphs of simple cubic functions, the reciprocal function		Unit 1, Unit 3
	$y = \frac{1}{x}$ with $x \neq 0$, the function $y = k^x$ for integer		
	values of x and simple positive values of k, the trigonometric functions $y = \sin x$ and $y = \cos x$		
A q	Construct the graphs of simple loci		Unit 3
Ar	Construct linear, quadratic and other functions from real-life problems and plot their corresponding graphs	Unit 2	Unit 2, Unit 3
As	Discuss, plot and interpret graphs (which may be non-linear) modelling real situations	Unit 1, Unit 2, Unit 3	Unit 1, Unit 2, Unit 3
At	Generate points and plot graphs of simple quadratic functions, and use these to find approximate solutions	Unit 3	Unit 3
Au	Direct and inverse proportion		Unit 3
Αv	Transformation of functions		Unit 3

Ref	Content descriptor	Unit	
Geometry		Foundation	Higher
GM a	Recall and use properties of angles at a point, angles on a straight line (including right angles), perpendicular lines, and opposite angles at a vertex	Unit 1, Unit 2	Unit 1, Unit 2
GM b	Understand and use the angle properties of intersecting lines, triangles and quadrilaterals	Unit 2	Unit 2
GM c	Calculate and use the sums of the interior and exterior angles of polygons	Unit 3	Unit 2
GM d	Recall the properties and definitions of special types of quadrilateral, including square, rectangle, parallelogram, trapezium, kite and rhombus	Unit 2	Unit 2
GM e	Recognise reflection and rotation symmetry of 2-D shapes	Unit 2	Unit 2
GM f	Understand congruence and similarity	Unit 2, Unit 3	Unit 3
GM g	Use Pythagoras' theorem in 2-D and 3-D	Unit 3	Unit 3
GM h	Use the trigonometric ratios and the sine and cosine rules to solve 2-D and 3-D problems		Unit 3
GM i	Distinguish between centre, radius, chord, diameter, circumference, tangent, arc, sector and segment	Unit 2	Unit 2
GM j	Understand and construct geometrical proofs using circle theorems		Unit 2, Unit 3
GM k	Use 2-D representations of 3-D shapes	Unit 2, Unit 3	Unit 2
GM I	Describe and transform 2-D shapes using single or combined rotations, reflections, translations, or enlargements by a positive then fractional or negative scale factors and distinguish properties that are preserved under particular transformations	Unit 3	Unit 3
GM v	Use straight edge and a pair of compasses to do constructions	Unit 3	Unit 3
GM w	Construct loci	Unit 3	Unit 3
GM x	Calculate perimeters and areas of shapes made from triangles and rectangles and other shapes	Unit 2	Unit 2

Ref	Content descriptor	Unit	
Geometry		Foundation	Higher
GM y	Calculate the area of a triangle using $\frac{1}{2}ab \sin C$		Unit 3
GM z	Find circumferences and areas of circles	Unit 3	Unit 3
GM aa	Calculate volumes of right prisms and shapes made from cubes and cuboids	Unit 2, Unit 3	Unit 2, Unit 3
GM bb	Solve mensuration problems involving more complex shapes and solids		Unit 3
GM cc	Use vectors to solve problems		Unit 3

Ref	Content descriptor	Unit	
Measur	Measures		Higher
GM m	Use and interpret maps and scale drawings	Unit 3	Unit 3
GM n	Understand and use the effect of enlargement for perimeter, area and volume of shapes and solids	Unit 3	Unit 3
GM o	Interpret scales on a range of measuring instruments and recognise the inaccuracy of measurements	Unit 1, Unit 2	Unit 1, Unit 2
GM p	Convert measurements from one unit to another	Unit 1, Unit 2, Unit 3	Unit 1, Unit 2, Unit 3
GM q	Make sensible estimates of a range of measures	Unit 1, Unit 2	Unit 1, Unit 2
GM r	Understand and use bearings	Unit 3	Unit 3
GM s	Understand and use compound measures	Unit 2	Unit 2, Unit 3
GM t	Measure and draw lines and angles	Unit 1, Unit 2	Unit 1, Unit 2
GM u	Draw triangles and other 2-D shapes using ruler and protractor	Unit 3	Unit 3

Ref	Content descriptor Unit		
Statisti	CS	Foundation	Higher
SP a	Understand and use statistical problem solving process/handling data cycle	Unit 1	Unit 1
SP b	Identify possible sources of bias	Unit 1	Unit 1
SP c	Design an experiment or survey, including sampling	Unit 1	Unit 1
SP d	Design data-collection sheets distinguishing between different types of data	Unit 1	Unit 1
SP e	Extract data from printed tables and lists	Unit 1	Unit 1
SP f	Design and use two-way tables for discrete and grouped data	Unit 1	Unit 1
SP g	Produce charts and diagrams for various data types	Unit 1	Unit 1
SP h	Calculate median, mean, range, quartiles and interquartile range, mode and modal class	Unit 1	Unit 1
SP i	Interpret a wide range of graphs and diagrams and draw conclusions	Unit 1	Unit 1
SP j	Look at data to find patterns and exceptions	Unit 1	Unit 1
SP k	Recognise correlation and draw and/or use lines of best fit by eye, understanding what these represent	Unit 1	Unit 1
SP I	Compare distributions and make inferences	Unit 1	Unit 1
SP u	Use calculators efficiently and effectively, including statistical functions	Unit 1	Unit 1

Ref	Content descriptor Unit		
Probab	ility	Foundation	Higher
SP m	Understand and use the vocabulary of probability and probability scale	Unit 1	Unit 1
SP n	Understand and use estimates or measures of probability from theoretical models (including equally likely outcomes), or from relative frequency	Unit 1	Unit 1
SP o	List all outcomes for single events, and for two successive events, in a systematic way and derive relative probabilities	Unit 1	Unit 1
SP p	Identify different mutually exclusive outcomes and know that the sum of the probabilities of all these outcomes is 1	Unit 1	Unit 1
SP q	Know when to add or multiply two probabilities: when <i>A</i> and <i>B</i> are mutually exclusive, then the probability of <i>A</i> or <i>B</i> occurring is $P(A) + P(B)$, whereas when <i>A</i> and <i>B</i> are independent events, the probability of <i>A</i> and <i>B</i> occurring is $P(A) \times P(B)$		Unit 1
SP r	Use tree diagrams to represent outcomes of compound events, recognising when events are independent		Unit 1
SP s	Compare experimental data and theoretical probabilities	Unit 1	Unit 1
SP t	Understand that if they repeat an experiment, they may – and usually will – get different outcomes, and that increasing sample size generally leads to better estimates of probability and population characteristics	Unit 1	Unit 1

Unit 1: Statistics and Probability

Foundation

Overview

Content overview

This unit contains:

1. Statistics

- Handling data cycle
- Data collection
- Data representation
- Analysing data
- Interpreting data

2. Probability

- Probability measures
- Relative frequency and theoretical probability
- Mutually exclusive outcomes

3. Number

- Four operations
- Decimals
- Percentages
- Equivalent fractions
- Accuracy
- Use of calculators

4. Algebra

- Notation
- Graphs

5. Geometry and Measures

- Angles at a point
- Scales and units

Assessment overview

- 30% of the qualification
- One written paper
- 1 hour 15 minutes
- 60 marks
- Answer all questions
- Calculator allowed
- Grades C-G available
- Available June and November
- 30–40% of the paper assesses the functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

1 Statistics

What students need to learn:

Ref	Content descriptor	Concepts and skills
SP a	Understand and use statistical	Specify the problem and plan
	problem solving process/handling data cycle	 Decide what data to collect and what statistical analysis is needed
		Collect data from a variety of suitable primary and secondary sources
		Use suitable data collection techniques
		Process and represent the data
		Interpret and discuss the data
SP b	Identify possible sources of bias	 Understand how sources of data may be biased
SP c	Design an experiment or survey	 Identify which primary data they need to collect including grouped data
		Consider fairness
		Understand sample and population
		Design a question for a questionnaire
		Criticise questions for a questionnaire
SP d	Design data-collection sheets distinguishing between different	 Design and use data-collection sheets for grouped, discrete and continuous data
	types of data	Collect data using various methods
		 Sort, classify and tabulate data and discrete or continuous quantitative data
		 Group discrete and continuous data into class intervals of equal width
SP e	Extract data from printed tables and lists	Extract data from lists and tables
SP f	Design and use two-way tables for discrete and grouped data	 Design and use two-way tables for discrete and grouped data
		Use information to complete a two-way table

Ref	Content descriptor	Concepts and skills
SP g	Produce charts and diagrams for	Produce
	various data types	– Pictograms
		– Bar charts
		– Pie charts
		 Histograms with equal class intervals
		 Frequency diagrams for grouped discrete data
		 Scatter graphs
		 Line graphs
		 Frequency polygons for grouped data
		 Ordered stem and leaf diagrams
		 Composite bar charts
		 Comparative and dual bar charts
SP h	Calculate median, mean, range, mode and modal class	Calculate:
		– mean
		– mode
		– median
		– range
		– modal class
		 interval containing the median
	•	 Estimate the mean of grouped data using the mid-interval value
		 Find the median for large data sets with grouped data
		 Estimate the mean for large data sets with grouped data
		 Understand that the expression 'estimate' will be used where appropriate, when finding the mean of grouped data using mid-interval values
		(NB: Quartiles and interquartile range are Higher Tier only)

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Ref	Content descriptor	Concepts and skills
SP i	Interpret a wide range of graphs	Interpret:
	and diagrams and draw	 composite bar charts
	conclusions	 comparative and dual bar charts
		– pie charts
		 stem and leaf diagrams
		 scatter graphs
		 frequency polygons
		 Recognise simple patterns, characteristics and relationships in bar charts, line graphs and frequency polygons
		 From pictograms, bar charts, line graphs, frequency polygons and frequency diagrams
		 read off frequency values
		 calculate total population
		 find greatest and least values
		From pie charts
		 find the total frequency
		 find the size of each category
_		 Find range, mode, median and greatest and least values from stem and leaf diagrams
SP j	Look at data to find patterns and exceptions	 Present findings from databases, tables and charts
		 Look at data to find patterns and exceptions
SP k	Recognise correlation and draw and/or use lines of best fit by eye,	 Draw lines of best fit by eye, understanding what these represent
	understanding what these represent	 Distinguish between positive, negative and zero correlation using lines of best fit
		 Understand that correlation does not imply causality
		 Use a line of best fit to predict values of a variable given the values of another variable

Content descriptor	Concepts and skills
Compare distributions and make inferences	Compare the mean and range of two distributions
	 Understand that the frequency represented by corresponding sectors in two pie charts dependent on the total populations represented by each of the pie charts
	 Use dual or comparative bar charts to compare distributions
	 Recognise the advantages and disadvantages between measures of average
Use calculators efficiently and effectively, including statistical functions	 Calculate the mean of a small data set, using the appropriate key on a scientific calculator
	inferences Use calculators efficiently and effectively, including statistical

2 Probability

What students need to learn:

Ref	Content descriptor	Concepts and skills
SP m	Understand and use the vocabulary of probability and probability scale	 Distinguish between events which are; impossible, unlikely, equal chance, likely, and certain to occur
		 Mark events and/or probabilities on a probability scale of 0 to 1
		 Write probabilities in words or fractions, decimals and percentages
SP n	Understand and use estimates or measures of probability from	 Find the probability of an event happening using theoretical probability
	theoretical models (including equally likely outcomes), or	 Find the probability of an event happening using relative frequency
	from relative frequency	 Estimate the number of times an event will occur, given the probability and the number of trials
		 Use theoretical models to include outcomes using dice, spinners, coins
SP o	List all outcomes for single events, and for two successive events, in a systematic way and derive relative probabilities	List all outcomes for single events systematically
		 List all outcomes for two successive events systematically
		Use and draw sample space diagrams
SP p	Identify different mutually exclusive outcomes and know that the sum of the probabilities of all these outcomes is 1	Add simple probabilities
		 Identify different mutually exclusive outcomes and know that the sum of the probabilities of all outcomes is 1
		 Use 1 - p as the probability of an event not occurring where p is the probability of the event occurring
		• Find a missing probability from a list or table
SP s	Compare experimental data and theoretical probabilities	 Compare experimental data and theoretical probabilities
SP t	Understand that if they repeat an experiment, they may – and usually will – get different outcomes, and that increasing sample size generally leads to better estimates of probability and population characteristics	Compare relative frequencies from samples of different sizes

3 Number

What students need to learn:

Ref	Content descriptor	Concepts and skills
N a	Add, subtract, multiply and divide any number	 Add, subtract, multiply and divide whole numbers, negative numbers, integers and decimals
		 Add and subtract mentally numbers with up to two decimal places
		- Recall all multiplication facts to 10 \times 10, and use them to derive quickly the corresponding division facts
		 Multiply and divide any number by powers of 10
		 Multiply or divide by any number between 0 and 1
		 Solve a problem involving division by a decimal (up to two decimal places)
N h	Understand equivalent fractions, simplifying a fraction by cancelling all common factors	Find equivalent fractions
		Write a fraction in its simplest form
		Compare fractions
Nj	Use decimal notation and recognise that each terminating decimal is a fraction	Understand place value
		 Convert between fractions and decimals using a calculator
ΝΙ	Understand that 'percentage'	Order fractions, decimals and percentages
	means 'number of parts per 100' and use this to compare proportions	 Convert between fractions, decimals and percentages
N m	Use percentage	Use percentage to solve problems
		Simple interest
No	Interpret fractions, decimals	Find a fraction of a quantity
	and percentages as operators	 Find a percentage of a quantity
		 Use decimals to find quantities
		Use a multiplier to increase or decrease

Ref	Content descriptor	Concepts and skills
Np	Use ratio notation, including reduction to its simplest form and its various links to fraction notation	Use ratiosWrite ratios in their simplest form
Nq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of	 Multiply and divide numbers using the commutative, associative, and distributive laws and factorisation where possible, or place value adjustments
	operations	Use inverse operations
		• Use brackets and the hierarchy of operations
		Solve word problems
Νt	Divide a quantity in a given ratio	• Divide a quantity in a given ratio
		Solve a ratio problem in context
Nu	Approximate to specified or appropriate degrees of accuracy including a given power of ten, number of decimal places and significant figures	Round numbers to a given power of 10
		 Round to the nearest integer and to a given number of significant figures
		Round to a given number of decimal places
	Significant figures	 Round to the nearest integer and to a giver number of significant figures Round to a given number of decimal places Estimate answers to calculations, including use of rounding Know how to enter complex calculations
Νv	Use calculators effectively and	Know how to enter complex calculations
	efficiently	 Enter a range of calculations including those involving time and money
		 Understand and interpret the calculator display, knowing when the display has been rounded by the calculator, and know not to round during the intermediate steps of a calculation
		• Use a range of calculator functions including $+, -, \times, \div, x^2, \sqrt{x}$, memory, $x^{\nu}, x^{1/\nu}$ and brackets

Algebra 4

What students need to learn:

Ref	Content descriptor	Concepts and skills	
A a	Distinguish the different roles played by letter symbols in algebra, using the correct notation	Use notation and symbols correctly	
Ab	Distinguish in meaning between	Write an expression	
	the words 'equation', 'formula' and 'expression'	 Select an expression/equation/formula from list 	n a
AI	Recognise and plot equations that correspond to straight line graphs in the coordinate plane, including finding gradients	• Recognise that equations in the form $y = mx$ corresponds to straight line graphs in the coordinate plane	; + c
		• Find the gradient of a straight line from a graph	
As	Discuss, plot and interpret graphs (which may be non-	• Interpret straight-line graphs for real-life situations	
	linear) modelling real situations	 Ready reckoner graphs 	
		 Conversion graphs 	
		– Fuel bills	
		 Fixed charge (standing charge) and cosper unit 	st

5 Geometry and Measures

What students need to learn:

Ref	Content descriptor	Concepts and skills
GM a	Recall and use properties of angles at a point	Recall and use properties of angles at a point
GM o	Interpret scales on a range of measuring instruments and recognise the inaccuracy of measurements	 Interpret scales on a range of measuring instruments
		 seconds, minutes, hours, days, weeks, months and years
		 Use correct notation for time, 12- and 24-hour clock
		Work out time intervals
		Recognise the inaccuracy of measurements
		 Know that measurements using real numbers depend on the choice of unit
		 Recognise that measurements given to the nearest whole unit may be inaccurate by up to one half in either direction
GM p	Convert measurements from one unit to another	Convert between metric units
GM q	Make sensible estimates of a range of measures	 Make sensible estimates of a range of measures in everyday settings
		 Choose appropriate units for estimating or carrying out measurements
GM t	Measure and draw lines and	 Measure and draw lines to the nearest mm
	angles	 Measure and draw angles to the nearest degree

Unit 2: Number, Algebra, Geometry 1

Foundation

Overview

Content overview

This unit contains:

1. Number

- The four operations
- Factors and multiples
- Squares, cubes and roots
- Index laws
- Fractions, decimals and percentages
- Inverse operations
- Recurring decimals
- Finding percentages
- Ratio
- Accuracy
- 2. Algebra
 - Expressions
 - Factorising
 - Sequences
 - Formulae
 - Coordinates in 2-D
 - Straight line graphs
 - Real-life graphs

3. Geometry

- Angles and triangles
- Symmetry
- Parallel lines
- Quadrilaterals
- Perimeter and area
- 3-D shapes
- Area and volume
- Parts of a circle

4. Measures

- Scales and units
- Compound measures

Assessment overview

- 30% of the qualification
- One written paper
- 1 hour 15 minutes
- 60 marks
- Answer all questions
- Non-calculator
- Grades G-C available
- Available June and November
- 30-40% of the paper assesses the functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

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1 Number

Ref	Content descriptor	Со	oncepts and skills
N a	Add, subtract, multiply and divide any number	•	Add, subtract, multiply and divide whole numbers, integers, fractions and decimals
		•	Derive and use positive integer complements to 100
		•	Add and subtract mentally numbers with up to two decimal places
		•	Recall all multiplication facts to 10×10 , and use them to derive quickly the corresponding division facts
		•	Multiply and divide any number by powers of 10
		•	Multiply or divide by any number between 0 and 1
		•	Solve a problem involving division by a decimal (up to two decimal places)
		•	Add, subtract, multiply and divide negative numbers
		•	Write numbers in words
		•	Write numbers from words
Nb	Order rational numbers	•	Order integers, decimals and fractions
		•	Understand and use positive numbers and negative integers, both as positions and translations on a number line
Nс	Use the concepts and vocabulary of factor (divisor), multiple, common factor, Highest Common Factor	•	Recognise even and odd numbers
		•	Identify factors, multiples and prime numbers from a list of numbers
	(HCF), Least Common Multiple (LCM), prime number and prime factor decomposition	•	Find the prime factor decomposition of positive integers
		•	Find common factors and common multiples of two numbers
		•	Find the Lowest common multiple (LCM) and Highest common factor (HCF) of two numbers

Ref	Content descriptor	Concepts and skills
N d	Use the terms square, positive and negative square root, cube and cube root	- Recall integer squares from 2 \times 2 up to 15 \times 15 and the corresponding square roots
	cube root	• Recall the cubes of 2, 3, 4, 5 and 10
		Find squares and cubes
		Find square roots and cube roots
Nе	Use index notation for squares,	Use index notation for squares and cubes
	cubes and powers of 10	Use index notation for powers of 10
		• Find the value of calculations using indices
N f	Use index laws for multiplication and division of integer powers	 Use index laws to simplify and calculate the value of numerical expressions involving multiplication and division of integer powers, and of powers of a power
		(NB: Fractional, zero and negative powers are only assessed on Higher Tier)
N h	Understand equivalent fractions, simplifying a fraction by cancelling all common factors	Find equivalent fractions
		Write a fraction in its simplest form
		 Convert between mixed numbers and improper fractions
		Compare fractions
Ni	Add and subtract fractions	Add and subtract fractions
Νj	Use decimal notation and recognise that each terminating decimal is a fraction	Understand place value
		 Identify the value of digits in a decimals
		Write terminating decimals as fractions
		 Recall the fraction-to-decimal conversion of familiar simple fractions
		Convert between fractions and decimals
Nk	Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals	 Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals
		 Convert between recurring decimals and fractions
ΝΙ	Understand that 'percentage'	Order fractions, decimals and percentages
	means 'number of parts per 100' and use this to compare proportions	 Convert between fractions, decimals and percentages

Ref	Content descriptor	Concepts and skills
Νο	Interpret fractions, decimals and percentages as operators	 Calculate a fraction of a given quantity Find a percentage of a quantity Use decimals to find quantities Use a multiplier to increase or decrease
Np	Use ratio notation, including reduction to its simplest form and its various links to fraction notation	Use ratiosWrite ratios in their simplest form
Νq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of operations	 Multiply and divide numbers using the commutative, associative, and distributive laws and factorisation where possible, or place value adjustments Use inverse operations
		 Use brackets and the hierarchy of operations
		 Use one calculation to find the answer to another
		Solve word problems
Νt	Divide a quantity in a given ratio	Divide a quantity in a given ratio
		Solve a ratio problem in context
Nu	Approximate to specified or	 Round numbers to a given power of 10
	appropriate degrees of accuracy including a given power of ten,	 Round to the nearest integer and to a given number of significant figures
	number of decimal places and significant figures	Round to a given number of decimal places
		 Estimate answers to calculations, including use of rounding

2 Algebra

Ref	Content descriptor	Concepts and skills
Аа	Distinguish the different roles played by letter symbols in algebra, using the correct notation	Use notation and symbols correctly
Ab	Distinguish in meaning between	Write an expression
	the words 'equation', 'formula' and 'expression'	 Select an expression/equation/formula from a list
Аc	Manipulate algebraic expressions by collecting like terms, by	Manipulate algebraic expressions by collecting like terms
	multiplying a single term over a bracket, and by taking out common	 Multiply a single algebraic term over a bracket
	factors	Write expressions to solve problems
		Write expressions using squares and cubes
		 Factorise algebraic expressions by taking out common factors
		Use simple instances of index laws
		(NB: Multiplying two linear expressions, factorising quadratic expressions including the difference of two squares and simplifying rational expressions are assessed at Higher Tier only)
A f	Derive a formula, substitute numbers into a formula	 Derive a simple formula, including those with squares, cubes and roots
		 Use formulae from mathematics and other subjects expressed initially in words and then using letters and symbols
		 Substitute numbers into a linear formula or simple formulae using indices
		• Substitute positive and negative numbers into expressions such as $3x^2 + 4$ and $2x^3$
Ai	Generate terms of a sequence using term-to-term and position-	Recognise sequences of odd and even numbers
	to-term definitions of the sequence	 Generate simple sequences of numbers, squared integers and sequences derived from diagrams
		 Write the term-to-term definition of a sequence in words
		 Find a specific term in the sequence using position-to-term or term-to-term rules
		• Identify which terms cannot be in a sequence

Ref	Content descriptor	Concepts and skills
Аj	Use linear expressions to describe the n^{th} term of an arithmetic sequence	 Find the <i>n</i>th term of an arithmetic sequence Use the <i>n</i>th term of an arithmetic sequence
Ak	Use the conventions for coordinates in the plane and plot points in all four quadrants,	 Use axes and coordinates to specify points in all four quadrants
		 Identify points with given coordinates
	including using geometric information	 Identify coordinates of given points
		(NB: Points may be in the first quadrant or all four quadrants)
		 Find the coordinates of points identified by geometrical information in 2-D
		• Find the coordinates of the midpoint of a line segment
ΑΙ	Recognise and plot equations that correspond to straight-line graphs in the coordinate plane, including finding gradients	Draw, label and scale axes
		 Recognise that equations of the form y = mx + c correspond to straight-line graphs in the coordinate plane
		 Plot and draw graphs of functions
		 Plot and draw graphs of straight lines of the form y = mx + c
		 Find the gradient of a straight line from a graph
A r	Construct linear functions from real-life problems and plot their	 Draw straight line graphs for real-life situations
	corresponding graphs	 Ready reckoner graphs
		 Conversion graphs
		– Fuel bills
		 Fixed charge (standing charge) and cost per unit
		Draw distance-time graphs
		(NB: Quadratic functions from real-life situations are assessed at Higher Tier only)

Ref	Content descriptor	Concepts and skills
(which may be no	Discuss, plot and interpret graphs (which may be non-linear)	 Interpret straight-line graphs for real-life situations
	modelling real situations	 Ready reckoner graphs
		 Conversion graphs
		– Fuel bills
		 Fixed charge (standing charge) and cost per unit
	•	 Interpret distance-time graphs

3 Geometry

Ref	Content descriptor	C	oncepts and skills
GM a	Recall and use properties of	٠	Recall and use properties of:
	angles at a point, angles on a straight line (including right		 angles at a point
	angles), perpendicular lines, and opposite angles at a vertex	 angles at a point on a straight line, including right angles 	 angles at a point on a straight line, including right angles
			 perpendicular lines
			 vertically opposite angles
		•	Find the size of the missing angles at a point or at a point on a straight line
		•	Distinguish between acute, obtuse, reflex and right angles
		٠	Name angles
		•	Estimate sizes of angles
		•	Give reasons for calculations
		•	Use two letter notation for a line and three letter notation for an angle
		٠	Mark perpendicular lines on a diagram
		٠	Identify a line perpendicular to a given line
		٠	Use geometric language appropriately
		٠	Use letters to identify points, lines and angles

Ref	Content descriptor	Concepts and skills
GM b	Understand and use the angle properties of parallel and	 Understand and use the angle properties of parallel lines
	intersecting lines, triangles and	Mark parallel lines on a diagram
	quadrilaterals	 Find missing angles using properties of corresponding and alternate angles
		 Understand and use the angle properties of quadrilaterals
		 Give reasons for angle calculations
		 Use the fact that angle sum of a quadrilateral is 360°
		 Understand the proof that the angle sum of a triangle is 180°
		 Find a missing angle in a triangle, using the angle sum of a triangle is 180°
		 Understand a proof that the exterior angle of a triangle is equal to the sum of the interior angles at the other two vertices
		 Distinguish between scalene, equilateral, isosceles and right-angled triangles
		 Understand and use the angle properties of triangles
		 Understand and use the angle properties of intersecting lines
		 Use the side/angle properties of isosceles and equilateral triangles
def	Recall the properties and definitions of special types of quadrilateral, including square,	 Recall the properties and definitions of special types of quadrilaterals, including symmetry properties
	rectangle, parallelogram, trapezium, kite and rhombus	 List the properties of each, or identify (name) a given shape
		Draw sketches of shapes
		 Name all quadrilaterals that have a specific property
		Identify quadrilaterals from everyday usage
		 Classify quadrilaterals by their geometric properties

Ref	Content descriptor	Concepts and skills
GM e	Recognise reflection and rotation symmetry of 2-D shapes	 Recognise reflection symmetry of 2-D shapes Identify and draw lines of symmetry on a
	Shapes	shapeRecognise rotation symmetry of 2-D shapes
		 Identify the order of rotational symmetry of a 2-D shape
		 Draw or complete diagrams with a given number of lines of symmetry
		 State the line symmetry as a simple algebraic equation
		 Draw or complete diagrams with a given order of rotational symmetry
GM f	Understand congruence and similarity	Understand similarity
		 Recognise that all corresponding angles are equal in size when the lengths of the sides are not
GM i	Distinguish between centre, radius, chord, diameter,	 Recall the definition of a circle and identify (name) and draw these parts of a circle
	circumference, tangent, arc,	 Understand related terms of a circle
	sector and segment	Draw a circle given the radius or diameter
GM k	Use 2-D representations of 3-D shapes	 Identify and name common solids: cube, cuboid, cylinder, prism, pyramid, sphere and cone
		 Know the terms face, edge and vertex
		 Use 2-D representations of 3-D shapes
		Use isometric grids

Ref	Content descriptor	Со	oncepts and skills
GM x	Calculate perimeters and areas	٠	Measure shapes to find perimeters and areas
	of shapes made from triangles	•	Find the perimeter of rectangles and triangles
	and rectangles	•	Find the perimeter of compound shapes
		٠	Find the area of a rectangle and triangle
		•	Calculate areas of compound shapes
		•	Find the area of a trapezium
		•	Find the area of a parallelogram
		•	Find surface area using rectangles and triangles
		•	Find the surface area of a prism
GM aa	Calculate volumes of right prisms and shapes made from	•	Find the volume of prisms, including a triangular prism, cube and cuboid
	cubes and cuboids	•	Recall and use the formula for the volume of a cuboid

4 Measures

Ref	Content descriptor	Concepts and skills	
GM o	Interpret scales on a range of	Indicate given values on a scale	
	measuring instruments and recognise the inaccuracy of measurements	 Interpret scales on a range of measuring instruments 	
		 seconds, minutes, hours, days, weeks, months and years 	
		 mm, cm, m, km, ml, cl, l, mg, g, kg, tonnes, °C 	
		 Use correct notation for time, 12- and 24-hour clock 	
		Work out time intervals	
		 Know that measurements using real numb depend on the choice of unit 	ers
		 Recognise that measurements given to the nearest whole unit may be inaccurate by u to one half in either direction 	
GM p	Convert measurements from one unit to another	 Convert between units of measure within a system 	one
		Convert metric units to metric units	
		(Metric equivalents should be known)	
		Convert imperial units to imperial units	
		(NB: Conversion between imperial units will be given)	е
		 Know rough metric equivalents of pounds, feet, miles, pints and gallons 	
		Metric Imperial	
		1 kg 2.2 pounds	
		$1 / 1 \frac{3}{4}$ pints	
		4.5 / 1 gallon	
		8 km 5 miles	
		30 cm 1 foot	
		 Convert between metric and imperial measures 	
		Estimate conversions	
		 Convert between speed measures, using metric units 	

Ref	Content descriptor	Concepts and skills
GM q	Make sensible estimates of a range of measures	 Make sensible estimates of a range of measures in everyday settings
		 Choose appropriate units for estimating or carrying out measurement
GM s	Understand and use compound measures	 Understand and use compound measures, including speed
		(NB: Density is Higher Tier only)
GM t	Measure and draw lines and	Measure and draw lines to the nearest mm
	angles	 Measure and draw angles to the nearest degree

Unit 3: Number, Algebra, Geometry 2

Foundation

Overview

Content overview

This unit contains:

1. Number

- Using percentages
- Reciprocals
- Using calculators

2. Algebra

- Equations
- Changing the subject of a formula
- Inequalities
- Trial and improvement
- Coordinates
- Straight line graphs
- Quadratic graphs

3. Geometry

- Polygons
- Pythagoras' theorem
- Congruence and similarity
- Transformations
- Constructions
- Drawing 3-D shapes
- Loci
- Circles and mensuration
- Prisms

4. Measures

- Bearings
- Scale drawings

Assessment overview

- 40% of the qualification
- One written paper
- 1 hour 30 minutes
- 80 marks
- Answer all questions
- Calculator allowed
- Grades C-G available
- Available in June and November
- 30-40% of the paper assesses the Functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

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1 Number

Ref	Content descriptor	Concepts and skills
Na	Add, subtract, multiply and divide any number	 Add, subtract, multiply and divide whole numbers, integers, negative numbers, fractions, decimals and numbers in index form
		 Recall the fraction-to-decimal conversion of familiar simple fractions
N m	Use percentage	 Find a percentage of a quantity in order to increase or decrease
		Use percentages in real-life situations
		– VAT
		 Value of profit or loss
		 Simple Interest
		 Income tax calculations
		 Annual rate of inflation
		(NB: Repeated proportional change is only assessed at Higher Tier)
Νo	Interpret fractions, decimals and percentages as operators	 Express a given number as a fraction of another
		 Express a given number as a percentage of another number
		Interpret percentage as an operator
		 Understand the multiplicative nature of percentages as operators
		 Use a multiplier to increase or decrease by a percentage in any scenario where percentages are used
Νq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of operations	 Understand 'reciprocal' as multiplicative inverse, knowing that any non-zero number multiplied by its reciprocal is 1 (and that zero has no reciprocal, because division by zero is not defined)
		Find reciprocals
		Use inverse operations
		 Understand and use unit fractions as multiplicative inverses

Ref	Content descriptor	Concepts and skills
Νv	Use calculators effectively and efficiently	 Use a calculator effectively and efficiently by entering a range of calculations including those involving time and money
		 Know how to enter complex calculations and use function keys, including +, -, ×, ÷, x², √x, memory, x^y, x^{1/y} and brackets

2 Algebra

Ref	Content descriptor	Concepts and skills
Аc	Manipulate algebraic expressions	Use algebraic manipulation to solve problems
by collecting like terms, by multiplying a single term over bracket, and by taking out co factors		(NB: Multiplying two linear expressions, factorising quadratic expressions including the difference of two squares and simplifying rational expressions are assessed at Higher Tier only)
A d	Set up and solve simple equations	Set up simple equations
		Rearrange simple equations
		Solve simple equations
		 Solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides of the equation
		 Solve linear equations which contain brackets, including those that have negative signs occurring anywhere in the equation, and those with a negative solution
		 Solve linear equations in one unknown, with integer and fractional coefficients
		(NB: Simultaneous equations in two unknowns is assessed at Higher Tier only)
A f	Substitute numbers into a formula	Substitute numbers into a formula
	and change the subject of a formula	 Change the subject of a formula (Having the new subject on both sides of the original formula is Higher Tier only)
		(NB: Rearranging of formula using square roots or squares is Higher Tier only)

Ref	Content descriptor	Concepts and skills
Ag	Solve linear inequalities in one variable, and represent the solution set on a number line	 Solve simple linear inequalities in one variable, and represent the solution set on a number line
		 Use the correct notation to show inclusive and exclusive inequalities
		(NB: Linear inequalities in two variables with suitable diagrammatic representation is assessed at Higher Tier only)
A h	Use systematic trial and improvement to find approximate solutions of equations where there is no simple analytical method of solving them	 Use systematic trial and improvement to find approximate solutions of equations where there is no simple analytical method of solving them
Ak	Use the conventions for coordinates in the plane and plot points in all four quadrants, including using geometric information	Calculate the length of a line segment
As	Discuss, plot and interpret graphs	Plot a linear graph
	(which may be non-linear) modelling real situations	 Interpret information presented in a range of linear and non-linear graphs
At	Generate points and plot graphs of simple quadratic functions, and use these to find approximate solutions	 Generate points and plot graphs of simple quadratic functions, then more general quadratic functions
		 Use the graph to solve approximate solutions of a quadratic equation from the graph of the corresponding quadratic function

3 Geometry

Ref	Content descriptor	Concepts and skills
GM c	Calculate and use the sums of the interior and exterior and	 Calculate and use the sums of the interior angles of polygons
	of polygons	 Use geometrical language appropriately and recognise and name pentagons, hexagons, heptagons, octagons and decagons
		• Use the sum of angles in irregular polygons
		 Calculate and use the angles of regular polygons
		 Use the sum of the interior angles of an <i>n</i>-sided polygon
		 Use the sum of the exterior angles of any polygon is 360°
		 Use the sum of the interior angle and the exterior angle is 180°
		 Use tessellations of regular and irregular polygons
		Tessellate combinations of polygons
		 Explain why some shapes tessellate and why other shapes do not
GM f	Understand congruence and similarity	Understand congruence
		 Identify shapes which are congruent
		Understand similarity
		 Identify shapes which are similar; including all circles or all regular polygons with equal number of sides
GM g	Use Pythagoras' theorem in 2-D	 Understand, recall and use Pythagoras' theorem in 2-D
GM k	Use 2-D representations of 3-D shapes	• Use 2-D representations of 3-D shapes
		 Draw nets and show how they fold to make a 3-D solid
		 Understand and draw front and side elevations and plans of shapes made from simple solids
		 Given the front and side elevations and the plan of a solid, draw a sketch of the 3-D solid

Ref Content descriptor

GM I Describe and transform 2-D shapes using single or combined rotations, reflections, translations, or enlargements by a positive scale factor and distinguish properties that are preserved under particular transformations

Concepts and skills

- Describe and transform 2-D shapes using single rotations
- Understand that rotations are specified by a centre and an (anticlockwise) angle
- Find the centre of rotation
- Rotate a shape about the origin, or any other point
- Describe and transform 2-D shapes using single reflections
- Understand that reflections are specified by a mirror line
- Identify the equation of a line of reflection
- Describe and transform 2-D shapes using single translations
- Understand that translations are specified by a distance and direction (using a vector)
 - Translate a given shape by the vector $\begin{pmatrix} 2\\ -3 \end{pmatrix}$
- Describe and transform 2-D shapes using enlargements by a positive scale factor
- Understand that an enlargement is specified by a centre and a scale factor
- Scale a shape on a grid (centre not specified)
- Draw an enlargement

•

- Enlarge a shape using (0, 0) as the centre of enlargement
- Enlarge shapes with a centre other than (0, 0)
- Find the centre of enlargement
- Describe and transform 2-D shapes using combined rotations, reflections, translations, or enlargements
- Distinguish properties that are preserved under particular transformations
- Recognise that enlargements preserve angle but not length
- Identify the scale factor of an enlargement of a shape as the ratio of the lengths of two corresponding sides

Ref	Content descriptor	C	oncepts and skills
GM I	(Continued)	•	Understand that distances and angles are preserved under rotations, reflections and translations, so that any figure is congruent under any of these transformations
GM v	Use straight edge and a pair of compasses to do constructions	•	Use straight edge and a pair of compasses to complete standard constructions
		•	Construct a triangle
		•	Construct an equilateral triangle
		•	Understand, from the experience of constructing them, that triangles satisfying SSS, SAS, ASA and RHS are unique, but SSA triangles are not
		•	Construct the perpendicular bisector of a given line
		•	Construct the perpendicular from a point to a line
		•	Construct the perpendicular from a point on a line
		•	Construct the bisector of a given angle
		•	Construct angles of 60° , 90° , 30° , 45°
		•	Draw parallel lines
		•	Draw circles and arcs to a given radius
		•	Construct a regular hexagon inside a circle
		•	Construct diagrams of everyday 2-D situations involving rectangles, triangles, perpendicular and parallel lines
		•	Draw and construct diagrams from given instructions

Ref	Content descriptor	Concepts and skills
GM w	Construct loci	Construct:
		 a region bounded by a circle and an intersecting line
		 a given distance from a point and a given distance from a line
		 equal distances from two points or two line segments
		 regions which may be defined by `nearer to' or `greater than'
		 Find and describe regions satisfying a combination of loci
		(NB: All loci restricted to two dimensions only)
GM z	Find circumferences and areas of circles	 Find circumferences of circles and areas enclosed by circles
		 Recall and use the formulae for the circumference of a circle and the area enclosed by a circle
		• Use $\pi \approx 3.142$ or use the π button on a calculator
		 Find the perimeters and areas of semicircles and quarter circles
		 Find the surface area of a cylinder
GM aa	Calculate volumes of right	Find the volume of a cylinder
	prisms and shapes made from cubes and cuboids	Use volume to solve problems

4 Measures

Ref	Content descriptor	Concepts and skills
GM m	Use and interpret maps and scale drawings	 Use and interpret maps and scale drawings Read and construct scale drawings Draw lines and shapes to scale Estimate lengths using a scale diagram
GM n	Understand the effect of enlargement for perimeter, area and volume of shapes	 Understand the effect of enlargement on perimeter, area and volume of shapes and solids
	and solids	Understand that enlargement does not have the same effect on area and volume
		 Use simple examples of the relationship between enlargement and areas and volumes of simple shapes and solids
GM p	Convert measurements from one unit to another	Convert between measures in the same system
		 Convert between area measures, using metric units
		 Convert between volume measures, using metric units
		 Convert between metric units of volume and units of capacity eg 1m/ = 1 cm³
GM r	Understand and use bearings	 Use three figure-bearings to specify direction
		• Mark on a diagram the position of point <i>B</i> given its bearing from point <i>A</i>
		 Draw or measure a bearing between the points on a map or scaled plan
		• Given the bearing of a point <i>A</i> from point <i>B</i> , work out the bearing of <i>B</i> from <i>A</i>
GM u	Draw triangles and other 2D shapes using ruler and protractor	 Make accurate drawing of triangles and other 2-D shapes using a ruler and a protractor
		 Make an accurate scale drawing from a diagram
		 Use accurate drawing to solve bearings problems

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Unit 1: Statistics and Probability

Higher

Overview

Content overview

This unit contains:

1. Statistics

- Handling data cycle
- Data collection
- Data Representation
- Analysing data
- Interpreting data
- Sampling
- Box plots, histograms and cumulative frequency

2. Probability

- Probability measures
- Relative probability
- Mutually exclusive outcomes
- Mutually exclusive and independent events
- Tree diagrams
- Addition and multiplication of probabilities

3. Number

- Four operations
- Decimals
- Percentages
- Equivalent fractions
- Compound interest
- Accuracy
- Use of calculators

4. Algebra

- Notation
- Graphs
- Graphs of functions

5. Geometry and Measures

- Angles at a point
- Scales and units

Assessment overview

- 30% of the qualification
- One written paper
- 1 hour 15 minutes
- 60 marks
- Answer all questions
- Calculator allowed
- Grades A*-D available (E allowed)
- Available in June and November
- 20-30% of the paper assesses the functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

Content that is Higher Tier only is indicated in **Bold type**.

The content of Foundation Tier is subsumed in the content for Higher Tier for that content descriptor.

1 Statistics

Ref	Content descriptor	Concepts and skills
SP a	Content descriptor Understand and use statistical problem solving process/handling data cycle Identify possible sources of bias	 Specify the problem and plan Decide what data to collect and what statistical analysis is needed Collect data from a variety of suitable primary and secondary sources Use suitable data collection techniques Process and represent the data Interpret and discuss the data Discuss how data relate to a problem, identify possible sources of bias and plan to minimise it
		 Understand how different sample sizes may affect the reliability of conclusions drawn
SP c	Design an experiment or survey	 Identify which primary data they need to collect including grouped data Consider fairness
		Understand sample and population
		 Design a question for a questionnaire
		Criticise questions for a questionnaire
		 Design an experiment or survey
		 Select and justify a sampling scheme and a method to investigate a population, including random and stratified sampling
		Use stratified sampling
SP d	Design data-collection sheets distinguishing between different types of data	 Design and use data-collection sheets for grouped, discrete and continuous data
		Collect data using various methods
		 Sort, classify and tabulate data and discrete or continuous quantitative data
		Group discrete and continuous data into class intervals of equal width
SP e	Extract data from printed tables and lists	Extract data from lists and tables

Unit 1 — Higher

Ref	Content descriptor	С	oncepts and skills
SP f	Design and use two-way tables for discrete and grouped data	٠	Design and use two-way tables for discrete and grouped data
		•	Use information provided to complete a two- way table
SP g	Produce charts and diagrams for	•	Produce:
	various data types		 Composite bar charts
			 Comparative and dual bar charts
			– Pie charts
			 Frequency polygons
			 Histograms with equal class intervals
			 Frequency diagrams for grouped discrete data
			 Scatter graphs
			– Line graphs
			 Frequency polygons for grouped data
			 Grouped frequency tables for continuous data
			 Ordered stem and leaf diagrams
			 Cumulative frequency tables
			 Cumulative frequency graphs
			 Box plots from raw data and when given quartiles, median
			 Histograms from class intervals with unequal width
		٠	Use and understand frequency density

Ref	Content descriptor	Concepts and skills
SP h	Calculate median, mean, range, quartiles and interquartile range, mode and modal class	 Calculate: mean, mode, median, range, modal class, interval containing the median Estimate the mean of grouped data using the mid-interval value
	 Find the median, quartiles and interquartile range for large data sets with grouped data 	
		 Estimate the mean for large data sets with grouped data
		 Understand that the expression 'estimate' will be used where appropriate, when finding the mean of grouped data using mid-interval values
		 Use cumulative frequency graphs to find median, quartiles and interquartile range
		 Interpret box plots to find median, quartiles, range and interquartile range

Ref	Content descriptor	Concepts and skills
SP i	Interpret a wide range of graphs and diagrams and draw conclusions	• Interpret:
		 composite bar charts
		 comparative and dual bar charts
		– pie charts
		 stem and leaf diagrams
		 scatter graphs
		 frequency polygons
		 box plots
		 cumulative frequency diagrams
		– histograms
		 Recognise simple patterns, characteristics and relationships in line graphs and frequency polygons
		 Find the median from a histogram or any other information from a histogram, such as the number of people in a given interval
		 From line graphs, frequency polygons and frequency diagrams
		 read off frequency values
		 calculate total population
		 find greatest and least values
		From pie charts:
		 find the total frequency
		 find the size of each section
		 Find the median, mode, range and interquartile range, as well as the greatest and least values from stem and leaf diagrams
		 From cumulative frequency graphs:
		 estimate frequency greater/less than a given value
		 find the median and quartile values and interquartile range
		From histograms:
		 complete a grouped frequency table
		 define the frequency density
		(NB: No pictograms or bar charts at Higher Tier)

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Ref	Content descriptor	Concepts and skills	
SP j	Look at data to find patterns and exceptions	Present findings from databases, tables an charts	d
		• Look at data to find patterns and exception	าร
		Explain an isolated point on a scatter graph	
SP k	Recognise correlation and draw and/or use lines of best fit by eye, understanding what these represent	• Draw lines of best fit by eye, understandin what these represent	g
		• Distinguish between positive, negative and zero correlation using lines of best fit	1
		Understand that correlation does not imply causality	1
		 Use a line of best fit, or otherwise, to predict values of a variable given values of the other variable 	F
		 Appreciate that correlation is a measu of the strength of the association between two variables and that zero correlation does not necessarily imply 'no relationship' but merely 'no linear relationship' 	
SP I	Compare distributions and make inferences	 Compare distributions and make inferences, using the shapes of distributions and measures of average and spread, including median and quartiles)
		 Compare the mean and range of two distributions, or median and interquarti range, as appropriate 	le
		• Understand that the frequency represented by corresponding sectors in two pie charts dependent upon the total populations represented by each of the pie charts	
		 Use dual or comparative bar charts to compare distributions 	
		Recognise the advantages and disadvantages between measures of average	jes
		 Compare the measures of spread between a pair of box plots/cumulativ frequency graphs 	'e
SP u	Use calculators efficiently and effectively, including statistical functions	• Calculate the mean of a small data set, usi the appropriate key on a scientific calculate	-
		• ∑ <i>x</i> and ∑ <i>fx</i> or the calculation of the line of best fit	e

2 Probability

Ref	Content descriptor	Concepts and skills
SP m	Understand and use the vocabulary of probability and probability scale	 Distinguish between events which are; impossible, unlikely, even chance, likely, and certain to occur
		 Mark events and/or probabilities on a probability scale of 0 to 1
		 Write probabilities in words or fractions, decimals and percentages
SP n	Understand and use estimates or measures of probability from theoretical models (including equally likely outcomes), or from relative frequency	 Understand and use estimates or measures of probability, including relative frequency
		 Use theoretical models to include outcomes using dice, spinners, coins
		 Find the probability of successive events, such as several throws of a single dice
		 Estimate the number of times an event will occur, given the probability and the number of trials
SP o	List all outcomes for single events, and for two successive events, in a systematic way and derive relative probabilities	 List all outcomes for single events, and for two successive events, systematically
		Use and draw sample space diagrams
SP p	Identify different mutually exclusive outcomes and know that the sum of the probabilities of all these outcomes is 1	Add simple probabilities
		 Identify different mutually exclusive outcomes and know that the sum of the probabilities of all these outcomes is 1
		 Use 1 – p as the probability of an event not occurring where p is the probability of the event occurring
		• Find a missing probability from a list or table
SP q	Know when to add or multiply two probabilities: when A and B are mutually exclusive, then the probability of A or B occurring is $P(A) + P(B)$, whereas when A and B are independent events, the probability of A and B occurring is $P(A) \times P(B)$	Use conditional probabilities
		 Understand selection with or without replacement

Ref	Content descriptor	С	oncepts and skills
SP r	Use tree diagrams to represent outcomes of compound events, recognising when events are independent	•	Draw a probability tree diagram based on given information (no more than 3 branches per event)
		•	Use a tree diagram to calculate conditional probability
SP s	Compare experimental data and theoretical probabilities	•	Compare experimental data and theoretical probabilities
SP t	Understand that if they repeat an experiment, they may – and usually will – get different outcomes, and that increasing sample size generally leads to better estimates of probability and population characteristics	•	Compare relative frequencies from samples of different sizes

Unit 1 — Higher

3 Number

Ref	Content descriptor	Concepts and skills
Na	Add, subtract, multiply and divide any number	 Add, subtract, multiply and divide whole numbers, negative numbers, integers, fractions and decimals
		 Multiply and divide by any number between 0 and 1
		Multiply and divide fractions
N h	Understand equivalent fractions, simplifying a fraction by	Find equivalent fractions
		Write a fraction in its simplest form
	cancelling all common factors	Compare fractions
Nj	Use decimal notation and recognise that each terminating decimal is a fraction	Convert between fractions and decimals
NI	Understand that 'percentage' means 'number of parts per 100' and use this to compare proportions	 Convert between fractions, decimals and percentages
N m	Use percentage, repeated proportional change	Use percentages to solve problems
		 Compound interest
		- Depreciation
Nо	Interpret fractions, decimals and percentages as operators	Find a fraction of a quantity
		Find a percentage of a quantity
		 Use decimals to find quantities
		 Use a multiplier to increase or decrease by a percentage in any scenario where percentages are used
Nр	Use ratio notation, including	Use ratios
-	reduction to its simplest form and its various links to fraction notation	Write ratios in their simplest form
Νq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of operations	 Multiply and divide numbers using the commutative, associative, and distributive laws and factorisation where possible, or place value adjustments
		Use inverse operations
		Use brackets and the hierarchy of operations
		Solve word problems

Ref	Content descriptor	Concepts and skills
Νt	Divide a quantity in a given ratio	Divide a quantity in a given ratio
		Solve a ratio problem in a context
Nu	Approximate to specified or	• Round numbers to a given power of 10
	appropriate degrees of accuracy including a given power of ten,	 Round to the nearest integer and to a given number of significant figures
	number of decimal places and significant figures	Round to a given number of decimal places
		 Estimate answers to calculations, including use of rounding
Νv	Use calculators effectively and efficiently	 Enter a range of calculations, including those involving time and money
	•	Know how to enter complex calculations
		 Understand and interpret the calculator display
		 Understand that premature rounding can cause problems when undertaking calculations with more than one step
		• Use calculator functions including +, -, ×, ÷, x^2 , \sqrt{x} , memory, x^y , $x^{1/y}$ and brackets

4 Algebra

Ref	Content descriptor	Concepts and skills
Aa	Distinguish the different roles played by letter symbols in algebra, using the correct notation	Use notation and symbols correctly
Ab	Distinguish in meaning between	Write an expression
	the words 'equation', 'formula', 'identity' and 'expression'	 Select an expression/identity/equation/ formula from a list
AI	Recognise and plot equations that correspond to straight-line graphs in the coordinate plane,	 Recognise that equations of the form y = mx + c correspond to straight-line graphs in the coordinate plane
	including finding gradients	 Find the gradient of a straight line from a graph
		 Analyse problems and use gradients to see how one variable changes in relation to another
A m	Understand that the form y = mx + c represents a straight line and that m is the gradient of the line and c is the value of the y - intercept	 Interpret and analyse a straight line graph
Ар	Recognise graphs of simple functions, including cubic, reciprocal and exponential curves	 Recognise a range of mathematical functions for lines of best fit and curves of best fit
As	Discuss, plot and interpret graphs (which may be non-	 Interpret straight line graphs for real-life situations
	linear) modelling real situations	 ready reckoner graphs
		 conversion graphs
		– fuel bills
		 fixed charge (standing charge) and cost per unit

5 Geometry and Measures

Ref	Content descriptor	Сс	oncepts and skills
GM a	Recall and use properties of angles at a point	•	Recall and use properties of angles at a point
GM o	Interpret scales on a range of measuring instruments and	•	Interpret scales on a range of measuring instruments
	recognise the inaccuracy of measurements		 seconds, minutes, hours, days, weeks, months and years
		•	Use correct notation for time, 12- and 24-hour clock
		•	Work out time intervals
		٠	Recognise the inaccuracy of measurements
		•	Know that measurements using real numbers depend on the choice of unit
		•	Recognise that measurements given to the nearest whole unit may be inaccurate by up to one half in either direction
GM p	Convert measurements from one unit to another	•	Convert metric units to metric units
GM q	Make sensible estimates of a range of measures	•	Make sensible estimates of a range of measures in everyday settings
		•	Choose appropriate units for estimating or carrying out estimates
GM t	Measure and draw lines and	•	Measure and draw lines to the nearest mm
	angles	•	Measure and draw angles, to the nearest degree

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Unit 2: Number, Algebra, Geometry 1

Higher

Overview

Content overview

This unit contains:

1. Number

- The four operations
- Factors and multiples
- Cubes, roots and squares
- Index Laws
- Standard form
- Surds
- Fractions, decimals and percentages
- Inverse operations
- Accuracy
- Recurring decimals
- Finding percentages
- Ratio

2. Algebra

- Expressions
- Factorising
- Formulae
- Rational expressions
- Sequences
- Coordinates in 2-D and 3-D
- Straight line graphs
- Gradients of lines
- Real life graphs

3. Geometry

- Angles and triangles
- Quadrilaterals
- Symmetry
- Polygons
- Parts of a circle
- Perimeter and area
- Circle theorems
- 3-D shapes
- Volume

4. Measures

- Scales and measures
- Compound measures

Assessment overview

- 30% of the qualification
- One written paper
- 1 hour 15 minutes
- 60 marks
- Answer all questions
- Non-Calculator
- Grades A*-D available (E allowed)
- Available June and November
- 20-30% of the paper assesses the functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

Content that is Higher Tier only is indicated in **Bold type**.

The content of Foundation Tier is subsumed in the content for Higher Tier for that content descriptor.

1 Number

Ref	Content descriptor	Concepts and skills	
Na	Add, subtract, multiply and divide any number	 Add, subtract, multiply and divide whole numbers, negative numbers, integers, fractions and decimals 	
		 Multiply and divide by any number between 0 and 1 	
Nb	Order rational numbers	Order integers, decimals and fractions	
		 Understand and use positive numbers and negative integers, both as positions and translations on a number line 	
Nс	Use the concepts and vocabulary of factor (divisor), multiple, common factor, Highest Common Factor, Least Common Multiple, prime number and prime factor decomposition	• Identify factors, multiples and prime number from a list of numbers	rs
		 Find the prime factor decomposition of positive integers 	
		 Find the common factors and common multiples of two numbers 	
		• Find the Highest Common Factor (HCF) and the Lowest Common Multiple (LCM) of two numbers	
N d	Use the terms square, positive and negative square root, cube and cube root	- Recall integer squares from 2 \times 2 to 15 \times 15 and the corresponding square roots	
		• Recall the cubes of 2, 3, 4, 5 and 10	
Nе	Use index notation for squares,	Use index notation for squares and cubes	
	cubes and powers of 10	• Use index notation for integer powers of 10	
		• Find the value of calculations which include indices	

Ref	Content descriptor	Со	oncepts and skills
N f	Use index laws for multiplication and division of integer, fractional and negative powers	•	Use index laws to simplify and calculate the value of numerical expressions involving multiplication and division of integer, fractional and negative powers, and powers of a power
		•	Recall that $n^0 = 1$ and $n^{-1} = \frac{1}{n}$ for positive
			integers n as well as, $n^{rac{1}{2}}=\sqrt{n}$ and
			$n^{\frac{1}{3}} = \sqrt[3]{n}$ for any positive number <i>n</i>
Ng	Interpret, order and calculate with numbers written in	•	Use standard form, expressed in conventional notation
	standard index form	•	Be able to write very large and very small numbers presented in a context in standard form
N h	Understand equivalent fractions, simplifying a fraction by cancelling all common factors	٠	Find equivalent fractions
		٠	Write a fraction in its simplest form
		٠	Convert between mixed numbers and improper fractions
Ni	Add and subtract fractions	•	Add and subtract fractions
Nj	Use decimal notation and recognise that each terminating decimal is a fraction	٠	Recall the fraction-to-decimal conversion of familiar simple fractions
		•	Convert between fractions and decimals
Nk	Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals	•	Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals
		•	Convert between recurring decimals and fractions
NI	Understand that 'percentage' means 'number of parts per 100' and use this to compare proportions	•	Convert between fractions, decimals and percentages
No	Interpret fractions, decimals and	•	Find a fraction of a quantity
	percentages as operators	•	Find percentages of quantities
		٠	Use decimals to find quantities
		•	Use a multiplier to increase or decrease
Nр	Use ratio notation, including	•	Use ratios
	reduction to its simplest form and its various links to fraction notation	•	Write ratios in their simplest form

Ref	Content descriptor	Cond	cepts and skills
Νq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of	co la	ultiply and divide numbers using the ommutative, associative, and distributive ws and factorisation where possible, or place alue adjustments
	operations	• U	se inverse operations
		• U	se brackets and the hierarchy of operations
		-	se one calculation to find the answer to nother
		• S	olve word problems
Νr	Use surds and π in exact calculations		se surds and π in exact calculations, vithout a calculator
			ive an answer to a question involving ne area of a circle as 25π
			ive an answer to use of Pythagoras' neorem as $\sqrt{13}$
		• W	/rite $(3 - \sqrt{3})^2$ in the form $a + b\sqrt{3}$
		• R	ationalise a denominator
Νt	Divide a quantity in a given ratio	• D	ivide a quantity in a given ratio
		• S	olve a ratio problem in a context
Nu	Approximate to specified or	• R	ound numbers to a given power of 10
	appropriate degrees of accuracy including a given power of ten,		ound to the nearest integer and to a given umber of significant figures
	number of decimal places and significant figures	• R	ound to a given number of decimal places
			stimate answers to calculations, including sing rounding

2 Algebra

Ref	Content descriptor	Concepts and skills
A a	Distinguish the different roles played by letter symbols in algebra, using the correct notation	Use notation and symbols correctly
Ab	Distinguish in meaning between	Write an expression
	the words 'equation', 'formula', 'identity' and 'expression'	 Select an expression/identity/equation/ formula from a list
Аc	Manipulate algebraic expressions by collecting like terms, by	 Manipulate algebraic expressions by collecting like terms
	multiplying a single term over a	 Multiply a single term over a bracket
	bracket, and by taking out common factors, multiplying two linear expressions, factorise quadratic	 Use instances of index laws, including use of fractional, zero and negative powers, and powers raised to a power
	expressions	 Factorise algebraic expressions by taking out common factors
		Write expressions to solve problems
		 Expand the product of two linear expressions
		Factorise quadratic expressions
		 Factorise quadratic expressions using the difference of two squares
		 Simplify rational expressions by cancelling, adding, subtracting, and multiplying
A f	Derive a formula, substitute numbers into a formula	Derive a formula
		 Use formulae from mathematics and other subjects
		Substitute numbers into a formula
		• Substitute positive and negative numbers into expressions such as $3x^2 + 4$ and $2x^3$
Ai	Generate terms of a sequence using term-to-term and position-	 Recognise sequences of odd and even numbers
	to-term definitions of the sequence	 Generate simple sequences of numbers, squared integers and sequences derived from diagrams
		 Describe the term-to-term definition of a sequence in words
		 Find a specific term in a sequence using the position-to-term and term-to-term rules
		Identify which terms cannot be in a sequence

Ref	Content descriptor	Concepts and skills
Аj	Use linear expressions to describe the n^{th} term of an arithmetic sequence	 Find the <i>n</i>th term of an arithmetic sequence Use the <i>n</i>th term of an arithmetic sequence
Ak	Use the conventions for coordinates in the plane and plot points in all four quadrants, including using geometric information	 Use axes and coordinates to specify points in all four quadrants in 2-D and 3-D Identify points with given coordinates Identify coordinates of given points (NB: Points may be in the first quadrant or all four quadrants) Find the coordinates of points identified by
		 geometrical information in 2-D and in 3-D Find the coordinates of the midpoint of a line segment
AI	Recognise and plot equations that correspond to straight-line graphs in the coordinate plane, including finding gradients	 Draw, label and scale axes Recognise that equations of the form y = mx + c correspond to straight-line graphs in the coordinate plane Plot and draw graphs of functions Plot and draw graphs of straight lines with equations of the form y = mx + c Find the gradient of a straight line from a graph
A m	Understand that the form y = mx + c represents a straight line and that m is the gradient of the line and c is the value of the y - intercept	 Understand that the form y = mx + c represents a straight line and that m is the gradient of the line and c is the value of the y - intercept Find the gradient of a straight line

Ref	Content descriptor	C	oncepts and skills
A n	Understand the gradients of parallel lines	٠	Explore the gradients of parallel lines and lines perpendicular to each other
		•	Write down the equation of a line parallel or perpendicular to a given line
		•	Select and use the fact that when y = mx + c is the equation of a straight line then the gradient of a line parallel to it will have a gradient of <i>m</i> and a line perpendicular to this line will have a
			gradient of $-\frac{1}{m}$
		•	Interpret and analyse a straight line graph and generate equations of lines parallel and perpendicular to the given line
A r	Construct linear functions from real-life problems and plot their corresponding graphs	•	Draw straight line graphs for real-life situations
			 ready reckoner graphs
			 conversion graphs
			- fuel bills
			 fixed charge (standing charge) and cost per unit
		٠	Draw distance-time graphs
A s	Discuss, plot and interpret graphs • (which may be non-linear)	•	Interpret straight line graphs for real-life situations
	modelling real situations		 Ready reckoner graphs
			 Conversion graphs
			– Fuel bills
			 Fixed charge (standing charge) and cost per unit
		•	Interpret distance-time graphs

3 Geometry

Ref	Content descriptor	Co	oncepts and skills	
GM a	Recall and use properties of angles at a point, on a straight line (including right angles), perpendicular lines, and opposite angles at a vertex	•	 Recall and use properties of angles angles at a point angles at a point on a straight line, 	
			 including right angles perpendicular lines vertically opposite angles 	
GM b	Understand and use the angle properties of intersecting lines	•	Distinguish between scalene, isosceles, equilateral, and right-angled triangles	
	and triangles	•	Understand and use the angle properties of triangles	
		•	Use the angle sum of a triangle is 180°	
		•	Understand and use the angle properties of intersecting lines	
		•	Understand and use the angle properties of parallel lines	
		٠	Mark parallel lines on a diagram	
		•	Use the properties of corresponding and alternate angles	
		•	Understand and use the angle properties of quadrilaterals	
		•	Give reasons for angle calculations	
		·	•	Explain why the angle sum of a quadrilateral is 360°
		•	Understand the proof that the angle sum of a triangle is 180°	
		•	Understand a proof that the exterior angle of a triangle is equal to the sum of the interior angles at the other two vertices	
		•	Recall and use these basic properties of angles in more complex problems	

Ref	Content descriptor	Concepts and skills
GM c	Calculate and use the sums of the interior and exterior angles of polygons	 Calculate and use the sums of the interior angles of polygons
		 Use geometrical language appropriately and recognise and name pentagons, hexagons, heptagons, octagons and decagons
		 Use the angle sum of irregular polygons
		 Calculate and use the angles of regular polygons
		 Use the sum of the interior angles of an n-sided polygon
		 Use the sum of the exterior angles of any polygon is 360°
		 Use the sum of the interior angle and the exterior angle is 180°
		 Find the size of each interior angle or the size of each exterior angle or the number of sides of a regular polygon
		 Understand tessellations of regular and irregular polygons
		 Tessellate combinations of polygons
		 Explain why some shapes tessellate and why other shapes do not
GM d	Recall the properties and definitions of special types of quadrilateral, including square, rectangle, parallelogram, trapezium, kite and rhombus	 Recall the properties and definitions of special types of quadrilateral, including symmetry properties
		 List the properties of each, or identify (name) a given shape
		 Classify quadrilaterals by their geometric properties
GM e	Recognise reflection and	Recognise reflection symmetry of 2-D shapes
	rotation symmetry of 2-D shapes	 Identify and draw lines of symmetry on a shape
		 Recognise rotation symmetry of 2-D shapes
		 Identify the order of rotational symmetry of a 2-D shape
		 Draw or complete diagrams with a given number of lines of symmetry
		 State the line of symmetry as a simple algebraic equation
		 Draw or complete diagrams with a given order of rotational symmetry

Ref	Content descriptor	Concepts and skills
GM i	Distinguish between centre, radius, chord, diameter,	• Recall the definition of a circle and identify (name) and draw the parts of a circle
	circumference, tangent, arc,	Understand related terms of a circle
	sector and segment	• Draw a circle given the radius or diameter
GM j	Understand and construct geometrical proofs using circle theorems	• Understand and use the fact that the tangent at any point on a circle is perpendicular to the radius at that point
		 Understand and use the fact that tangents from an external point are equal in length
		Find missing angles on diagrams
		 Give reasons for angle calculations involving the use of tangent theorems
GM k	Use 2-D representations of 3-D shapes	• Use 2-D representations of 3-D shapes
		Use isometric grids
		 Draw nets and show how they fold to make 3-D solid
		 Understand and draw front and side elevations and plans of shapes made from simple solids
		• Given the front and side elevations and the plan of a solid, draw a sketch of the 3-D sol

Ref	Content descriptor	Concepts and skills
GM x	Calculate perimeters and areas	Measure shapes to find perimeter or area
	of shapes made from triangles	• Find the perimeter of rectangles and triangles
	and rectangles, and other shapes	 Calculate perimeter and area of compound shapes made from triangles, rectangles and other shapes
		 Recall and use the formulae for the area of a triangle and a rectangle
		Calculate areas of compound shapes
		Find the area of a trapezium
		Find the area of a parallelogram
		 Find the surface area of simple shapes (prisms) using the formulae for triangles and rectangles, and other shapes
GM aa	Calculate volumes of right prisms and shapes made from cubes and cuboids	 Calculate volumes of right prisms, including triangular prisms, and shapes made from cubes and cuboids
		 Recall and use the formula for the volume of a cuboid

4 Measures

Ref	Content descriptor	С	oncepts a	nd skills
GM o	Interpret scales on a range of measuring instruments and recognise the inaccuracy of measurements	٠		t measurements using real numbers oon the choice of unit
		•	nearest w	e that measurements given to the hole unit may be inaccurate by up to n either direction
GM p	Convert measurements from one unit to another	٠	Convert b same syst	etween units of measure in the em
		•		ion between imperial units will be equivalents should be known)
		•		gh metric equivalents of pounds, s, pints and gallons:
			Metric	Imperial
			1 kg	2.2 pounds
			1/	$1\frac{3}{4}$ pints
			4.5 /	1 gallon
			8 km	5 miles
			30 cm	1 foot
		•	Convert b measures	etween imperial and metric
		٠	Convert b metric uni	etween speed measures, using its
				etween metric units of volume and apacity measures, eg 1 cm ³ = 1 m/
GM q	Make sensible estimates of a range of measures			sible estimates of a range of in everyday settings
		•	•	opropriate units for estimating or out estimates
GM s	Understand and use compound measures	•	Understar including	nd and use compound measures, speed
GM t	Measure and draw lines and	•	Measure a	and draw lines to the nearest mm
	angles	•	Measure a degree	and draw angles, to the nearest

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Unit 3: Number, Algebra, Geometry 2

Higher

Overview

Content overview

This unit contains:

1. Number

- Calculations with standard form
- **Proof with** recurring decimals
- Using percentage and repeated percentage change
- Compound interest
- Reciprocals
- Upper and lower bounds
- Using calculators
- 2. Algebra
 - Equations
 - Quadratic equations
 - Changing the subject of the formula
 - Inequalities
 - Trial and improvement
 - Simultaneous equations
 - Graphs of functions
 - Graphs of loci
 - Quadratic graphs
 - Direct and indirect proportion
 - Transformation of functions

3. Geometry

- Congruence
- Pythagoras' Theorem
- Trigonometry
- Circle theorems
- Transformations
- Constructions
- Loci
- $\frac{1}{2}ab \sin C$
- Mensuration
- Vectors

4. Measures

- Bearings
- Scale drawings

Assessment overview

- 40% of the qualification
- One written paper
- 1 hour 45 minutes
- 80 marks
- Answer all questions
- Calculator allowed
- Grades A*-D available (E allowed)
- Available June and November
- 20-30% of the papers assess the functional elements of Mathematics

References

Each topic in this unit contains a specification reference (for example, **SP a** for Statement a, Statistics and Probability), the content descriptor and examples of concepts and skills associated with that content descriptor.

Content at Higher Tier only is indicated in **Bold type**.

The content of Foundation Tier is subsumed in the content for Higher Tier for that content descriptor.

1 Number

Ref	Content descriptor	Concepts and skills
Na	Add, subtract, multiply and divide any number	 Add, subtract, multiply and divide whole numbers, integers, negative numbers, fractions and decimals, and numbers in index form
		 Solve a problem involving division by a decimal (up to 2 decimal places)
Ng	Interpret, order and calculate with numbers written in	Convert between ordinary and standard form representations
	standard index form	 Interpret a calculator display using standard form
		Calculate with standard form
Nk	Recognise that recurring decimals are exact fractions, and that some exact fractions are recurring decimals	Convert between recurring decimals and fractions
		 Understand a recurring decimal to fraction proof
Nm	Use percentage, repeated proportional change	Use percentages in real-life situations
		– VAT
		 Simple Interest
		 Income tax calculations
		 Compound interest
		- Depreciation
		 Find prices after a percentage increase or decrease
		 Percentage profit and loss
		 Calculate an original amount when given the transformed amount after a percentage change
		Calculate repeated proportional change

Unit 3 — Higher

Ref	Content descriptor	С	oncepts and skills
N n	Direct and indirect proportion	•	Calculate an unknown quantity from quantities that vary in direct or inverse proportion
No	Interpret fractions, decimals and percentages as operators	٠	Express a given number as a fraction of another number
		•	Express a given number as a percentage of another number
		•	Understand the multiplicative nature of percentages as operators
		•	Represent repeated proportional change using a multiplier raised to a power
		•	Use compound interest
		•	Use a multiplier to increase or decrease by a percentage in any scenario where percentages are used
Nq	Understand and use number operations and the relationships between them, including inverse operations and hierarchy of operations	•	Understand 'reciprocal' as multiplicative inverse, knowing that any non-zero number multiplied by its reciprocal is 1 (and that zero has no reciprocal, because division by zero is not defined)
	operations	•	Find reciprocals
		•	Use inverse operations
		•	Understand that the inverse operation of raising a positive number to a power n is raising the result of this operation to the power $\frac{1}{n}$
		٠	Understand and use unit fractions as multiplicative inverses
		•	Use reverse nercentage calculations

• Use reverse percentage calculations

Ref	Content descriptor	Сс	oncepts and skills
N s	Calculate upper and lower bounds	•	Calculate the upper and lower bounds of calculations, particularly when working with measurements
		•	Find the upper and lower bounds of calculations involving perimeter, areas and volumes of 2-D and 3-D shapes
		•	Find the upper and lower bounds in real life situations using measurements given to appropriate degrees of accuracy
		•	Give the final answer to an appropriate degree of accuracy following an analysis of the upper and lower bounds of a calculation
Νv	Use calculators effectively and efficiently, including trigonometrical functions	•	Use an extended range of calculator functions including $+, -, \times, \div, x^2, \sqrt{x}$, memory, $x^y, x^{1/y}$, brackets and trigonometrical functions
		•	Calculate the upper and lower bounds of calculations, particularly when working with measurements
		•	Use standard form display and know how to enter numbers in standard form
		•	Calculate using standard form
		•	Use calculators for reverse percentage calculations by doing an appropriate division
		•	Use calculators to explore exponential growth and decay, using a multiplier and the power key

2 Algebra

Ref	Content descriptor	С	oncepts and skills
Ac	Manipulate algebraic expressions by collecting like terms, by multiplying a single term over a bracket, and by taking out common factors, multiplying two linear expressions, factorise quadratic expressions including the difference of two squares and simplify rational expressions	•	Use algebraic manipulation to solve problems
A d	Set up and solve simple equations	•	Set up simple equations
	including simultaneous	•	Rearrange simple equations
	equations in two unknowns	٠	Solve simple equations
		•	Solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides of the equation
		•	Solve linear equations which contain brackets, including those that have negative signs occurring anywhere in the equation, and those with a negative solution
		•	Solve linear equations in one unknown, with integer or fractional coefficients
		•	Find the exact solutions of two simultaneous equations in two unknowns
		•	Be able to use elimination or substitution to solve simultaneous equations
		•	Interpret a pair of simultaneous equations as a pair of straight lines and their solution as the point of intersection on a graph
		•	Set up and solve a pair of simultaneous equations in two variables
Ae	Solve quadratic equations	•	Solve simple quadratic equations by using the quadratic formula
		•	Solve simple quadratic equations by factorisation and completing the square
A f	Substitute numbers into a formula	•	Substitute numbers into a formula
	and change the subject of a formula	•	Change the subject of a formula including cases where the subject occurs on both sides of the formula, or where a power of the subject appears

Ref	Content descriptor	Concepts and skills
Ag	Solve linear inequalities in one or two variables, and represent the solution set on a number line or	 Solve simple linear inequalities in one variable, and represent the solution set on a number line
	coordinate grid	 Use the correct notation to show inclusive and exclusive inequalities
		 Show the solution set of several inequalities in two variables on a graph
A h	Use systematic trial and improvement to find approximate solutions of equations where there is no simple analytical method of solving them	 Use systematic trial and improvement to find approximate solutions of equations where there is no simple analytical method of solving them
Ak	Use the conventions for coordinates in the plane and plot points in all four quadrants, including using geometric information	Calculate the length of a line segment
AI	Recognise and plot equations that correspond to straight-line graphs in the coordinate plane, including finding gradients	 Find the gradient of lines given by equations of the form y = mx + c
		 Analyse problems and use gradients to see how one variable changes in relation to another
Αο	Find the intersection points of the graphs of a linear and quadratic function, knowing that these are the approximate solutions of the corresponding simultaneous equations representing the linear and quadratic functions	• Solve exactly, by elimination of an unknown, two simultaneous equations in two unknowns, one of which is linear in each unknown, and the other is linear in one unknown and quadratic in the other, or where the second equation is of the form $x^2 + y^2 = r^2$
		 Find approximate solutions to simultaneous equations formed from one linear function and one quadratic function using a graphical approach
		 Select and apply algebraic and graphical techniques to solve simultaneous equations where one is linear and one quadratic

Ref	Content descriptor	Concepts and skills
Ар	Draw, sketch, recognise graphs of simple cubic functions, the	• Plot graphs of simple cubic functions, the
		reciprocal function $y = \frac{1}{x}$ with $x \neq 0$,
	reciprocal function $y = \frac{1}{x}$ with $x \neq 0$, the function $y = k^x$ for integer values of x and simple positive values of k , the trigonometric functions	the exponential function $y = k^x$ for integer values of x and simple positive values of k, the trigonometric functions $y = \sin x$ and $y = \cos x_r$ within the range -360° to +360°
	$y = \sin x$ and $y = \cos x$	 Recognise the characteristic shapes of all these functions
		 Draw and plot a range of mathematical functions
		 Interpret and analyse a range of mathematical functions and be able to draw them, recognising that they are of the correct shape
A q	Construct the graphs of simple loci	 Construct the graphs of simple loci including the circle x² + y² = r² for a circle of radius r centred at the origin of coordinates
		 Find graphically the intersection points of a given straight line with this circle
		 Select and apply construction techniques and understanding of loci to draw graphs based on circles and perpendicular lines
A r	Construct linear, quadratic and other functions from real-life problems and plot their	 Generate points and plot graphs of simple quadratic functions, then more general quadratic functions
	corresponding graphs	 Find approximate solutions of a quadratic equation from the graph of the corresponding quadratic function
		 Find the intersection points of the graphs of a linear and a quadratic function, knowing that these are the approximate solutions of the corresponding simultaneous equations representing the linear and quadratic functions
As	Discuss, plot and interpret graphs	Plot a linear graph
	(which may be non-linear) modelling real situations	 Interpret information presented in a range of linear and non-linear graphs

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Ref	Content descriptor	Сс	oncepts and skills
At	Generate points and plot graphs of simple quadratic functions, and use these to find approximate solutions	•	Generate points and plot graphs of simple quadratic functions, then more general quadratic functions
		•	Find approximate solutions of a quadratic equation from the graph of the corresponding quadratic function
		•	Select and use the correct mathematical techniques to draw quadratic graphs
A u	Direct and inverse proportion	•	Set up and use equations to solve word and other problems involving direct proportion or inverse proportion and relate algebraic solutions to graphical representation of the equations
Αv	Transformation of functions	•	Apply to the graph of $y = f(x)$ the transformations $y = f(x) + a$, $y = f(ax)$, y = f(x + a), $y = af(x)$ for linear, quadratic, sine and cosine functions $f(x)$
		•	Select and apply the transformations of reflection, rotation, enlargement and translation of functions expressed algebraically
		•	Interpret and analyse transformations of functions and write the functions algebraically

3 Geometry

What students need to learn:

Ref	Content descriptor	Concepts and skills
GM f	Understand congruence and similarity	 Recognise that all corresponding angles in similar figures are equal in size when the lengths of sides are not
		 Understand and use SSS, SAS, ASA and RHS conditions to prove the congruence of triangles using formal arguments, and to verify standard ruler and a pair of compasses constructions
		 Understand similarity of triangles and of other plane figures, and use this to make geometric inferences
		 Formal geometric proof of similarity of two given triangles
GM g	Use Pythagoras' theorem in 2-D and 3-D	 Understand, recall and use Pythagoras' theorem in 2-D, then in 3-D problems
		 Understand the language of planes, and recognise the diagonals of a cuboid
		 Calculate the length of a diagonal of a cuboid
GM h	Use the trigonometric ratios and the sine and cosine rules to solve 2-D and 3-D problems	• Use the trigonometric ratios to solve 2-D and 3-D problems
		 Understand, recall and use trigonometric relationships in right-angled triangles, and use these to solve problems in 2-D and in 3-D configurations
		 Find the angle between a line and a plane (but not the angle between two planes or between two skew lines)
		 Find angles of elevation and angles of depression
		 Use the sine and cosine rules to solve 2-D and 3-D problems

Specification issue 3

Ref	Content descriptor	Сс	oncepts and skills
GM j	Understand and construct geometrical proofs using circle theorems	٠	Prove and use the facts that:
			 the angle subtended by an arc at the centre of a circle is twice the angle subtended at any point on the circumference
			 the angle in a semicircle is a right angle
			 angles in the same segment are equal
			 opposite angles of a cyclic quadrilateral sum to 180°
			 alternate segment theorem
			 the perpendicular from the centre of a circle to a chord bisect the chord
GM I	Describe and transform 2-D shapes using single or combined rotations, reflections, translations, or enlargements by a positive fractional or negative scale factor and distinguish properties that are preserved under particular transformations	•	Describe and transform 2-D shapes using single rotations
		•	Understand that rotations are specified by a centre and an (anticlockwise) angle
		٠	Find the centre of rotation
		•	Rotate a shape about the origin, or any other point
		•	Describe and transform 2-D shapes using single reflections
		•	Understand that reflections are specified by a mirror line
		•	Identify the equation of a mirror line of symmetry
		•	Describe and transform 2-D shapes using single translations
		•	Understand that translations are specified by a distance and direction (using a vector)
		•	Translate a given shape by the vector $\begin{pmatrix} 2\\ -3 \end{pmatrix}$

Ref	Content descriptor	Concepts and skills
GM I	(Continued)	 Describe and transform 2-D shapes using enlargements by a positive and/or a negative or fractional scale factor
		 Understand that an enlargement is specified by a centre and a scale factor
		 Enlarge a shape using (0, 0) as the centre of enlargement
		• Enlargement with centre other than (0, 0)
		 Find the centre of enlargement
		 Describe and transform 2-D shapes using combined rotations, reflections, translations, or enlargements
		 Distinguish properties that are preserved under particular transformations
		 Recognise that enlargements preserve angle but not length
		 Use congruence to show that translation, rotations and reflections preserve length and angle, so that any figure is congruent to its image under any of these transformations
		 Understand that distances and angles are preserved under rotations, reflections and translations so that any shape is congruent to its image
		Describe a transformation

Ref	Content descriptor	Concepts and skills
GM v	Use straight edge and a pair of compasses to do constructions	 Use straight edge and a pair of compasses to do standard constructions
		Construct a triangle
		Construct an equilateral triangle
		 Understand, from the experience of constructing them, that triangles satisfying SSS, SAS, ASA and RHS are unique, but SSA triangles are not
		 Construct the perpendicular bisector of a given line
		 Construct the perpendicular from a point to a line
		 Construct the perpendicular from a point on a line
		Construct the bisector of a given angle
		 Construct angles of 60°, 90°, 30°, 45°
		Draw parallel lines
		• Draw circles and arcs to a given radius
		Construct a regular hexagon inside a circle
		 Construct diagrams of everyday 2-D situations involving rectangles, triangles, perpendicular and parallel lines
		 Draw and construct diagrams from given information
GM w	Construct loci	Construct
		 a region bounded by a circle and an intersecting line
		 a given distance from a point and a given distance from a line
		 equal distances from two points or two line segments
		 regions which may be defined by `nearer to' or `greater than'
		 Find and describe regions satisfying a combination of loci
		(NB: All loci restricted to two dimensions only)
GM y	Calculate the area of a triangle using $\frac{1}{2}ab \sin C$	 Calculate the area of a triangle given the length of two sides and the included angle

Ref	Content descriptor	Concepts and skills		
GM z	Find circumferences and areas of circles	 Find circumferences of circles and areas enclosed by circles 		
		 Recall and use the formulae for the circumference of a circle and the area enclosed by a circle 		
		• Use $\pi \approx 3.142$ or use the π button on a calculator		
		 Find the perimeters and areas of semicircles and quarter circles 		
		 Calculate the lengths of arcs and the areas of sectors of circles 		
		• Answers in terms of π may be required		
		Find the surface area of a cylinder		
GM aa	Calculate volumes of right	Find the volume of a cylinder		
	prisms and shapes made from cubes and cuboids	Use volume to solve problems		
GM bb	Solve mensuration problems involving more complex shapes and solids	 Solve problems involving more complex shapes and solids, including segments of circles and frustums of cones 		
		 Find the surface areas and volumes of compound solids constructed from cubes, cuboids, cones, pyramids, spheres, hemispheres, cylinders 		
		Examples:		
		 Solve problems including examples of solids in everyday use 		
		 Find the area of a segment of a circle given the radius and length of the chord 		
GM cc	Use vectors to solve problems	 Understand and use vector notation 		
		 Calculate, and represent graphically, the sum of two vectors, the difference of two vectors and a scalar multiple of a vector 		
		Calculate the resultant of two vectors		
		 Solve geometrical problems in 2-D using vector methods 		
		 Apply vector methods for simple geometrical proofs 		

4 Measures

Ref	Content descriptor	Concepts and skills		
GM m	Use and interpret maps and scale drawings	 Use and interpret maps and scale drawings Read and construct scale drawings 		
		Draw lines and shapes to scaleEstimate lengths using a scale diagram		
GM n	Understand and use the effect of enlargement for perimeter, area and volume of shapes and solids	 Understand the effect of enlargement for perimeter, area and volume of shapes and solids 		
		 Understand that enlargement does not have the same effect on area and volume 		
		 Use simple examples of the relationship between enlargement and areas and volumes of simple shapes and solids 		
		 Use the effect of enlargement on areas and volumes of shapes and solids 		
		 Know the relationships between linear, area and volume scale factors of mathematically similar shapes and solids 		
GM p	Convert measurements from one unit to another	Convert between metric area measures		
		Convert between metric volume measures		
		 Convert between metric units of volume and units of capacity measures, eg 1m/ = 1 cm³ 		
GM r	Understand and use bearings	Use three-figure bearings to specify direction		
		 Mark on a diagram, the position of a point B given its bearing and distance from point A 		
		 Measure or draw a bearing between two points on a map or scaled plan 		
		• Given the bearing of a point <i>A</i> from a point <i>B</i> , work out the bearing of point <i>B</i> from point <i>A</i>		
GM s	Understand and use compound measures	 Understand and use compound measures, including density 		
GM u	Draw triangles and other 2-D shapes using ruler and protractor	 Make accurate drawing of triangles and other 2-D shapes using a ruler and a protractor 		
		 Make an accurate scale drawing from a diagram 		
		 Use accurate drawing to solve bearings problems 		

Assessment summary

Units 1, 2, and 3 are all externally assessed.

Unit 1:	Statistics and Probability	Unit code 1F: 5MB1F
		Unit code 1H: 5MB1H
 Extern 	ally assessed	
• One w	ritten paper	
• Includ	es elements of number, algebra, geometry and measures	s common with Unit 2
• 1 hour	15 minutes Foundation Tier	
• 1 hour	15 minutes Higher Tier	
• 60 ma	rks	
Calcula	ator allowed	
• Tiered	papers	
• Fo	undation Tier grades C-G available	
o Hig	gher Tier grades A*-D available (E allowed)	
o 30	-40% of Foundation Tier paper assesses the functional e	lements of Mathematics
o 20	-30% of Higher Tier paper assesses the functional eleme	ents of Mathematics

Unit 2:	Number, Algebra, Geometry 1	Unit code 2F: 5MB2F		
		Unit code 2H: 5MB2H		
• Externa	lly assessed			
One wri	tten paper			
• 1 hour	1 hour 15 minutes Foundation Tier			
• 1 hour	1 hour 15 minutes Higher Tier			
• 60 marl	• 60 marks			
Non-cal	Non-calculator			
Tiered p	papers			
∘ Fou	ndation Tier grades C-G available			
o Higl	ner Tier grades A*-D available (E allowed)			

- 30-40% of Foundation Tier paper assesses the functional elements of Mathematics 0
- 20-30% of Higher Tier paper assesses the functional elements of Mathematics 0

Unit 3: Number, Algebra, Geometry 2

Unit code 3F: 5MB3F Unit code 3H: 5MB3H

- Externally assessed
- One written paper
- 1 hour 30 minutes Foundation Tier
- 1 hour 45 minutes Higher Tier
- 80 marks
- Calculator allowed
- Tiered papers
 - Foundation Tier grades C-G available
 - Higher Tier grades A*-D available (E allowed)
 - $_{\odot}$ 30-40% of Foundation Tier paper assesses the functional elements of Mathematics
 - 20-30% of Higher Tier paper assesses the functional elements of Mathematics

Assessment Objectives and weightings

		% in GCSE
AO1:	Recall and use their knowledge of the prescribed content	45-55%
AO2:	Select and apply mathematical methods in a range of contexts	25-35%
AO3:	Interpret and analyse problems and generate strategies to solve them	15-25%
	TOTAL	100%

Relationship of Assessment Objectives to units

Unit	Assessment Objective			
	A01	A02	A03	Total for AO1, AO2 and AO3
Unit 1: Statistics and Probability	13.5-16.5%	7.5-10.5%	4.5-7.5%	30%
Unit 2: Number, Algebra, Geometry 1	13.5-16.5%	7.5-10.5%	4.5-7.5%	30%
Unit 3: Number, Algebra, Geometry 2	18-22%	10-14%	6-10%	40%
Total for GCSE	45-55%	25-35%	15-25%	100%

Entering your students for assessment

Student entry

From summer 2014 onwards students will be required to sit all their examinations at the end of the course.

Students may enter a unit at any tier of entry.

Details of how to enter students for this qualification can be found in *Edexcel's UK Information Manual*, a copy is sent to all examinations officers. The information can also be found on Edexcel's website (www.edexcel.com).

Forbidden combinations and classification code

Centres should be aware that students who enter for more than one GCSE qualification with the same classification code will have only one grade (the highest) counted for the purpose of the school and college performance tables.

Students should be advised that, if they take two qualifications with the same classification code, schools and colleges are very likely to take the view that they have achieved only one of the two GCSEs. The same view may be taken if students take two GCSE qualifications that have different classification codes but have significant overlap of content. Students who have any doubts about their subject combinations should check with the institution to which they wish to progress before embarking on their programmes.

Access arrangements and special requirements

Edexcel's policy on access arrangements and special considerations for GCE, GCSE and Entry Level is designed to ensure equal access to qualifications for all students (in compliance with the Equality Act 2010) without compromising the assessment of skills, knowledge, understanding or competence.

Please see the Edexcel website (www.edexcel.com) for:

- the JCQ policy Access Arrangements, Reasonable Adjustments and Special Considerations
- the forms to submit for requests for access arrangements and special considerations
- dates for submission of the forms.

Requests for access arrangements and special considerations must be addressed to:

Special Requirements Edexcel One90 High Holborn London WC1V 7BH

Equality Act 2010

Please see the Edexcel website (www.edexcel.com) for information with regard to the Equality Act 2010.

Assessing your students

The first assessment opportunity for all units of this qualification will take place in the June 2014 series and in each following June and November series for the lifetime of the specification.

Assessment opportunities

Unit	June/ November 2014	June/ November 2015	June/ November 2016	June/ November 2017
Unit 1	~	✓	✓	✓
Unit 2	~	✓	✓	✓
Unit 3	√	✓	✓	✓

Please note, first certification of this qualification is in **June 2014** and thereafter.

Awarding and reporting

The grading, awarding and certification of this qualification will comply with the requirements of the GCSE/GCE Code of Practice, which is published by the office of the Qualifications and Examinations Regulator (Ofqual). The GCSE qualification will be graded and certificated on an eight-grade scale from A* to G. Higher Tier units are awarded at grades A*-D, with E allowed. Foundation Tier units are awarded at grades C-G. Individual unit results will be reported.

The results for a student who fails to reach the minimum standard for a grade to be awarded will be recorded as U (Unclassified) and will not be certificated.

The first certification opportunity for the Edexcel GCSE in Mathematics B will be June 2014.

Unit results

The minimum uniform marks required for each grade for each unit:

Units 1 and 2

Unit grade	*A	А	В	С	D	E	F	G
Maximum uniform mark = 120	108	96	84	72	60	48	36	24

The maximum uniform mark available for students entered for the Foundation Tier unit is 83.

Students who do not achieve the standard required for a grade G will receive a uniform mark in the range 0-24.

Unit 3

Unit grade	*A	А	В	С	D	E	F	G
Maximum uniform mark = 160	144	128	112	96	80	64	48	32

The maximum uniform mark available for students entered for the Foundation Tier unit is 111.

Students who do not achieve the standard required for a grade G will receive a uniform mark in the range 0-31.

Qualification results

The minimum uniform marks required for each grade:

GCSE in Mathematics B	cash-in code: 2MB01							
Qualification grade	*A	А	В	С	D	E	F	G
Maximum uniform mark = 400	360	320	280	240	200	160	120	80

Students who do not achieve the standard required for a grade G will receive a uniform mark in the range 0-79.

Students may enter a unit at any tier of entry. However, the overall grade calculation will be based on their total uniform mark score.

Re-taking of qualifications

Students wishing to re-take a GCSE are required to re-take all the units in the qualification.

Language of assessment

Assessment of this specification will be available in English only. Assessment materials will be published in English only and all work submitted for examination must be produced in English.

Quality of written communication

Students will be assessed on their ability to:

- write legibly, with accurate use of spelling, grammar and punctuation in order to make the meaning clear
- select and use a form and style of writing appropriate to purpose and to complex subject matter
- organise relevant information clearly and coherently, using specialist vocabulary when appropriate.

Stretch and challenge

Students can be stretched and challenged in both units through the use of different assessment strategies, for example:

- using a variety of stems in questions for example: explain, find, calculate, compare, prove
- ensuring connectivity between parts of questions
- use of a wider range of question types to address different skills for example structured, non structured, task-based questions, prove etc
- students are challenged by the content, skills and knowledge defined in each unit of the specification.

GCSE in Mathematics will assess functional elements of mathematics, as required by the Key Stage 4 Programme of Study for Mathematics.

This will be 20-30% on Higher Tier papers, and 30-40% on Foundation Tier papers.

Malpractice and plagiarism

For up-to-date advice on malpractice and plagiarism, please refer to the Joint Council for Qualifications *Suspected Malpractice in Examinations: Policies and Procedures* document on the JCQ website www.jcq.org.uk

Student recruitment

Edexcel's access policy concerning recruitment to our qualifications is that:

- they must be available to anyone who is capable of reaching the required standard
- they must be free from barriers that restrict access and progression
- equal opportunities exist for all students.

Prior learning

This qualification builds on the content, knowledge and skills developed in the Key Stage 3 Programme of Study for Mathematics as defined by the National Curriculum Orders for England.

Progression

This GCSE in Mathematics B provides progression to Level 3 qualifications in numerate disciplines, such as:

- GCE Mathematics
- GCE Further Mathematics
- GCEs in the Science subjects
- GCE Geography
- other qualifications which require mathematical skills, knowledge and understanding.

This qualification also supports further training and employment where mathematical skills, knowledge and understanding is desirable.

Grade descriptions

Grade descriptions are provided to give a general indication of the standards of achievement likely to have been shown by candidates awarded particular grades. The descriptions must be interpreted in relation to the content in the specification; they are not designed to define that content.

The grade awarded will depend in practice upon the extent to which the candidate has met the Assessment Objectives overall. Shortcomings in some aspects of candidates' performance in the assessment may be balanced by better performances in others.

Grade A

Learners use a wide range of mathematical techniques, terminology, diagrams and symbols consistently, appropriately and accurately. Learners are able to use different representations effectively and they recognise equivalent representations for example numerical, graphical and algebraic representations. Their numerical skills are sound, they use a calculator effectively and they demonstrate algebraic fluency. They use trigonometry and geometrical properties to solve problems.

Learners identify and use mathematics accurately in a range of contexts. They evaluate the appropriateness, effectiveness and efficiency of different approaches. Learners choose methods of mathematical communication appropriate to the context. They are able to state the limitations of an approach or the accuracy of results. They use this information to inform conclusions within a mathematical or statistical problem.

Learners make and test hypotheses and conjectures. They adopt appropriate strategies to tackle problems (including those that are novel or unfamiliar), adjusting their approach when necessary. They tackle problems that bring together different aspects of mathematics and may involve multiple variables. They can identify some variables and investigate them systematically; the outcomes of which are used in solving the problem.

Learners communicate their chosen strategy. They can construct a rigorous argument, making inferences and drawing conclusions. They produce simple proofs and can identify errors in reasoning.

Grade C

Learners use a range of mathematical techniques, terminology, diagrams and symbols consistently, appropriately and accurately. Learners are able to use different representations effectively and they recognise some equivalent representations eg numerical, graphical and algebraic representations of linear functions; percentages, fractions and decimals. Their numerical skills are sound and they use a calculator accurately. They apply ideas of proportionality to numerical problems and use geometric properties of angles, lines and shapes.

Learners identify relevant information, select appropriate representations and apply appropriate methods and knowledge. They are able to move from one representation to another, in order to make sense of a situation. Learners use different methods of mathematical communication.

Learners tackle problems that bring aspects of mathematics together. They identify evidence that supports or refutes conjectures and hypotheses. They understand the limitations of evidence and sampling, and the difference between a mathematical argument and conclusions based on experimental evidence.

They identify strategies to solve problems involving a limited number of variables. They communicate their chosen strategy, making changes as necessary. They construct a mathematical argument and identify inconsistencies in a given argument or exceptions to a generalisation.

Grade F

Learners use some mathematical techniques, terminology, diagrams and symbols from the Foundation Tier consistently, appropriately and accurately. Learners use some different representations effectively and can select information from them. They complete straightforward calculations competently with and without a calculator. They use simple fractions and percentages, simple formulae and some geometric properties, including symmetry.

Learners work mathematically in everyday and meaningful contexts. They make use of diagrams and symbols to communicate mathematical ideas. Sometimes, they check the accuracy and reasonableness of their results.

Learners test simple hypotheses and conjectures based on evidence. Learners are able to use data to look for patterns and relationships. They state a generalisation arising from a set of results and identify counterexamples. They solve simple problems, some of which are non-routine.

C Resources, support and training

FREE Teacher Support Materials

Mathematics Emporium – an online filing cabinet with essential documents for teachers

Register online to gain access to our **Mathematics Emporium** – you'll find everything you need to support your students throughout the year, including: past papers, sample papers, mock papers and mark schemes.

To request free access, please visit **www.edexcelmaths.com**

Edexcel published resources

We have a comprehensive suite of resources to support our Mathematics specifications, written by senior examiners and practising teachers. They include:

- **Student Books**: differentiated and accessible text books to help all students make progress. We've combined ResultsPlus exam performance data with valuable examiner insight to give students lots of tips and guidance on how to achieve exam success.
- ActiveTeach: digital resources enriched with BBC Active video clips to engage all students.
- **Teacher Guides**: offering you complete support with teaching the specification. These contain easy-to-use lesson plans to save you valuable planning time.

If you would like to receive an evaluation pack for Edexcel GCSE Mathematics published resources (Specification A or B), please visit www.maths10.co.uk and click on the 'Resources' tab.

Training

A programme of professional development and training courses covering various aspects of the specification and examination will be arranged by Edexcel each year on a regional basis. We can also customise courses to your specific training needs, and deliver them at your centre or Local Authority.

Full details can be obtained from:

Training from Edexcel							
Edexcel							
One90 High Ho	lborn						
London WC1V 7BH							
Telephone:	0844 576 0027						
Email: trainingbookings@edexcel.com							
Website:	www.edexcel.com						

Edexcel support services

We have a wide range of support services to help you plan, teach and manage this qualification successfully.

From the maths team of Edexcel **email bulletins** are a fantastic way to be kept informed of all the developments that are taking place in mathematics. If you would like to be added to this email distribution list, please email **mathsemporium@edexcel.com**

ResultsPlus – our free online analysis service provides you with an in-depth analysis of how students performed in their exams on a question-by-question basis. Quick and easy to use, you can download exam performance data in Excel spreadsheets and reference papers, examiner reports and mark schemes. At a glance, you'll be able to see how well a specification is understood across the whole department.

ResultsPlus Skills Maps are available for GCSE Mathematics and go one step further with the analysis by mapping performance to specific areas of knowledge that are being tested. You can pinpoint areas for improvement to help you tailor revision for individual students.

For further information or find out how to access and use this service, please call 0844 576 0024 or visit **www.edexcel.com/resultsplus**

Ask the Expert – To make it easier for you to raise a query with us online, we have merged our **Ask Edexcel** and **Ask the Expert** services.

There is now one easy-to-use web query form that will allow you to ask any question about the delivery or teaching of Edexcel qualifications. You'll get a personal response, from one of our administrative or teaching experts, sent to the email address you provide.

We're always looking to improve the quantity and quality of information in our FAQ database, so you'll be able to find answers to many questions you might have by searching before you submit the question to us.

Support for Students

Learning flourishes when students take an active interest in their education; when they have all the information they need to make the right decisions about their futures. With the help of feedback from students and their teachers, we've developed a website for students that will help them:

- Understand subject specifications
- Access past papers and mark schemes
- Find out how to get exams remarked
- Learn about other students' experiences at university, on their travels and entering the workplace

We're committed to regularly updating and improving our online services for students. The most valuable service we can provide is helping schools and colleges unlock the potential of their learners. www.edexcel.com/students

Regional teams – Do you know your dedicated Curriculum Development Manager? Every school and college in the country has an allocated member of the Edexcel team, regionally based, who is available to provide support, help, advice and training for your curriculum offer.

Regional office telephone numbers are listed below:

Birmingham	0121 616 2585
Bristol	0117 950 1908
Cardiff	0292 079 4865
Leeds	0115 224 2253
Manchester	0161 855 7560

Endorsed resources

Edexcel also endorses some additional materials written to support this qualification. Any resources bearing the Edexcel logo have been through a quality assurance process to ensure complete and accurate support for the specification. For up-to-date information about endorsed resources, please visit www.edexcel.com/endorsed

Please note that while resources are checked at the time of publication, materials may be withdrawn from circulation and website locations may change.

D Appendices

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Appendix 1 Key skills

Signposting

Key skills (Level 2)	All units
Application of number	
N2.1	\checkmark (grade C standard or above)
N2.2	\checkmark (grade C standard or above)
N2.3	\checkmark (grade C standard or above)
Communication	
C2.1a	\checkmark
C2.1b	\checkmark
C2.2	✓
C2.3	✓
Information and communication technology (ICT)	
ICT2.1	✓
ICT2.2	✓
ICT2.3	✓
Improving own learning and performance	
LP2.1	\checkmark
LP2.2	✓
LP2.3	✓
Problem solving	
PS2.1	✓
PS2.2	\checkmark
PS2.3	✓
Working with others	
W02.1	✓
W02.2	\checkmark
W02.3	✓

Development suggestions

Please refer to the Edexcel website for key skills development suggestions.

Appendix 2 Wider curriculum

Signposting

Issue	All units
Spiritual	✓
Moral	✓
Ethical	✓
Social	✓
Legislative	✓
Economic	✓
Cultural	✓
Sustainable	✓
Health and safety	✓
European initiatives	✓

Development suggestions

Issue	Unit	Opportunities for development
Spiritual	All units	This qualification enables centres to provide courses in
Moral	All units	Mathematics that allow students to discriminate between truth and falsehood. As candidates explore mathematical
Ethical	All units	models of the real world there will be many naturally arising moral and cultural issues, environmental and health
Social	All units	and safety considerations and aspects of European
Legislative	All units	developments for discussion, for example:
Economic	All units	 use and abuse of statistics in the media
Cultural	All units	 financial and business mathematics
Sustainable	All units	 how mathematics is used to communicate climate change
Health and safety	All units	 cultural and historical roots of mathematics
European initiatives	All units	• use of mathematics in cultural symbols and patterns.

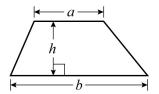
Appendix 3 Codes

Type of code	Use of code	Code number
National classification codes	Every qualification is assigned to a national classification code indicating the subject area to which it belongs. Centres should be aware that students who enter for more than one GCSE qualification with the same classification code will have only one grade (the highest) counted for the purpose of the school and college performance tables.	2210
National Qualifications	E ach qualification title is allocated a National Qualifications Framework (NQF) code.	The QN for the qualification in this publication is:
Framework (NQF) codes	The National Qualifications Framework (NQF) code is known as a Qualification Number (QN). This is the code that features in the DfE Section 96 and on the LARA as being eligible for 16–18 and 19+ funding, and is to be used for all qualification funding purposes. The QN is the number that will appear on the student's final certification documentation.	GCSE – 500/7886/0
Unit codes	Each unit is assigned a unit code. This unit code is used as an entry code to indicate that a student	Unit 1F – 5MB1F
	wishes to take the assessment for that unit. Centres	Unit 1H – 5MB1H
	will need to use the entry codes only when entering students for their examination.	Unit 2F – 5MB2F
		Unit 2H – 5MB2H
		Unit 3F – 5MB3F
		Unit 3H – 5MB3H
Cash-in codes	The cash-in code is used as an entry code to aggregate the student's unit scores to obtain the overall grade for the qualification. Centres will need to use the entry codes only when claiming students' qualifications.	GCSE – 2MB01
Entry codes	The entry codes are used to:	Please refer to the Edexcel
	enter a student for the assessment of a unit	UK Information Manual, available on the Edexcel
	• aggregate the student's unit scores to obtain the overall grade for the qualification.	website.

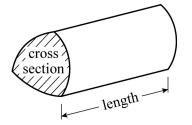
Appendix 4 Formulae sheets

Foundation Tier

Area of trapezium = $\frac{1}{2}(a+b)h$

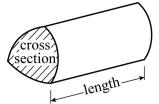


Volume of a prism = area of cross section × length



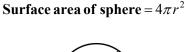
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Formulae: Higher Tier



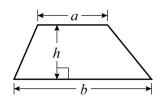
Volume of a prism = area of cross section \times length

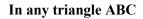
Volume of sphere = $\frac{4}{3}\pi r^3$

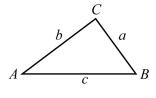




Area of trapezium = $\frac{1}{2}(a+b)h$







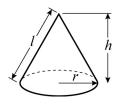
Sine Rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule $a^2 = b^2 + c^2 - 2bc\cos A$

Area of triangle = $\frac{1}{2}ab\sin C$

Volume of cone = $\frac{1}{3}\pi r^2 h$

Curved surface area of cone = πrl





The solutions of $ax^2 + bx + c = 0$ where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

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