



General Certificate of Education

Statistics 6380

SS02 Statistics unit 2

Mark Scheme

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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Key to mark scheme and abbreviations used in marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
✓ or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
− <i>x</i> EE	deduct <i>x</i> marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

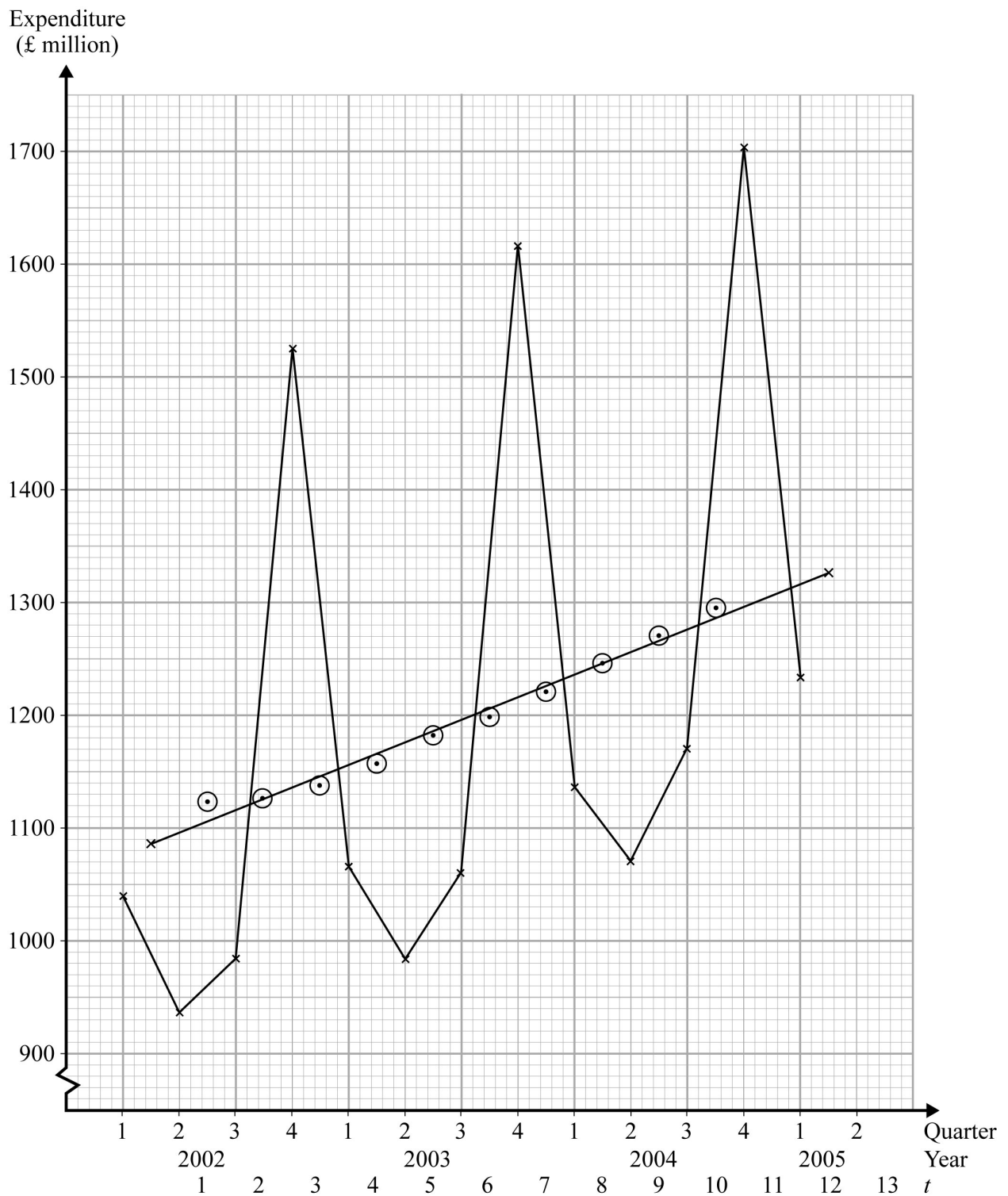
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

SS02

Q	Solution	Marks	Total	Comments
1(a)(i)	$P(3 \text{ or fewer})=0.779$	B1		0.779 (0.778~0.779)
(a)(ii)	$P(3)=P(3 \text{ or fewer})-P(2 \text{ or fewer})$ $=0.7787-0.5679$ $=0.209$	M1 m1 A1	4	$P(3)=P(\leq 3)-P(\leq 2)$ completely correct method 0.209 (0.208~0.21)
(b)	Poisson mean $5 \times 2.4=12$ $P(>10)=1-P(10 \text{ or fewer})$ $=1-0.3472$ $=0.653$	B1 M1 A1	3	Poisson mean 5×2.4 $P(>10)=1-P(10 \text{ or fewer})$ 0.653 (0.652~0.653)
(c)	No, customers are likely to join shortest queue i.e. not at random.	E1 E1	2	No Reason – allow not independent – couple may shop together etc.
	Total		9	
2(a)	$\frac{983+1059+1618+1135}{4} = 1199$	M1 A1	2	method 1199 (1198~1200)
(b)	on next page	M1 A1	2	m.a. in correct position Accurate plot – by eye – allow 1 small slip
(c)	$t = 0 \quad y = 1086$ $t = 12 \quad y = 1326$ + line	M1 A1	2	method for line accurate line drawn
(d)	residuals for Q2 –158, –193, –196 mean = –179	M1 m1 A1	3	method for residual – allow from graph – ignore sign – their line method for seasonal effect – ignore sign – allow omission of Q2,2002 –179 (–170~–200) 2 maximum if answered in (e)
(e)	$1086 + 12.5 \times 19.96 - 179$ $= 1335.5 - 179$ $= 1156.5$ forecast £1160 million	M1 M1 B1 B1✓	4	method for trend – allow them from graph – their line method for including their negative seasonal effect – their trend (1130~1170) allow 1100 or 1200 2 or 3 sf and £m Allow 3 maximum if method is not clear or based on Q2 results only
(f)	this is a poor forecast but no purely numerical method could have predicted Q2,2005 would be less than Q2,2004	E1 E1	2	poor forecast / ineffective method no numerical method could have forecast this result / extrapolation is inherently unreliable
	Total		15	

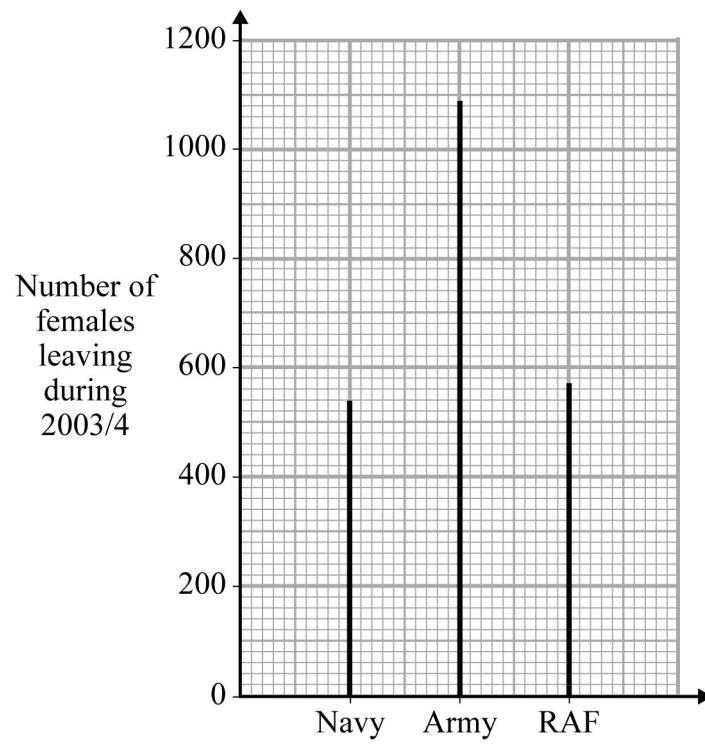
SS02 (cont)



SS02 (cont)

Q	Solution	Marks	Total	Comments
3(a)	$E(X) = 0 \times 0.32 + 1 \times 0.25 + 2 \times 0.19 + 3 \times 0.12 + 4 \times 0.09 + 5 \times 0.03$ $= 1.5$	M1 A1	5	method for $E(X)$ 1.5 CAO
	$E(X^2) = 0^2 \times 0.32 + 1^2 \times 0.25 + 2^2 \times 0.19 + 3^2 \times 0.12 + 4^2 \times 0.09 + 5^2 \times 0.03$ $= 4.28$	M1		method for $E(X^2)$ – may be implied
	$\text{Var}(X) = 4.28 - 1.5^2 = 2.03$	m1		method for s.d.; allow for variance = 2.03
	s.d. = $\sqrt{2.03}$ $= 1.42$	A1		1.42(1.41~1.43)
	(b)(i) s.d. = $\sqrt{2.2}$ $= 1.48$	M1		method
		A1		1.48(1.48~1.49)
(b)(ii)	more houses in Cheadle are advertised in the Clarion than in the Sentinel. The week to week variability is similar	E1✓		Clarion higher average
		E1	2	variability similar
(c)	choose Clarion – since more houses in Cheadle advertised on average	B1✓ B1	2	Clarion higher mean
	Total		11	
4(a)	15320	B1	1	15320 or 15300
(b)	$890 - 580 = 310$	M1	2	method
		A1		310 CAO
(c)	1998/9 to 2003/4	M1	2	method – allow small slip
		A1		1998/9 to 2003/4 CAO
(d)	on next page	M1	3	method – allow horizontal – allow bars instead of lines but not if joined
		B1		– disallow broken scale
		A1		axes labelled – generous accurate plot by eye
(e)(i)	$\frac{11950}{32130} \times 100 = 37.2\%$	M1		method for ratio
		A1		37.2(37~37.3)
(e)(ii)	more leaving than joining – in the long run this would lead to no one being left to leave	E1	3	explanation
	Total		11	

SS02 (cont)



SS02 (cont)

Q	Solution	Marks	Total	Comments
5(a)	number employees 0000 to 9319 select 4-digit random numbers ignore repeats and >9319 continue until 120 numbers obtained select corresponding employees	E1 E1 E1 E1	4	any valid numbering select 4-digit random numbers ignore repeats and >9319 (must be consistent in numbering) continue until 120 numbers obtained
(b)(i)	from each of the 4 chosen councils select a random sample of 30 employees	E1 E1	2	select a sample from each of the 4 councils of size 30
(b)(ii)	employees to be interviewed would be geographically localised / easier / cheaper	E2,1	2	reason – easier/cheaper without further explanation gets E1
(c)(i)	council / age / sex / length of service	B1B1	2	any sensible suggestion; B1 for each
(c)(ii)	More representative of population	E1	1	more representative allow all have equal chance
	Total		11	

SS02 (cont)

Q	Solution	Marks	Total	Comments
6(a)(i)	$H_0 : \mu = 41 \quad H_1 : \mu > 41$ $\bar{x} = 52.03$ $z = \frac{52.03 - 41}{\frac{8.5}{\sqrt{10}}} = 4.10$ c.v. 2.3263 reject H_0 : significant evidence that mean speed exceeds 41 mph non-standardised c.v. $41 + 2.3263 \times \left(\frac{8.5}{\sqrt{10}} \right) = 47.25$ compare with 52.03 confidence interval $52.03 \pm 2.3263 \times \frac{8.5}{\sqrt{10}}$ 45.78 ~ 58.28 compare 45.78 with 41 p-value compare 0.0000204 with 0.01	B1 B1 B1 M1 m1 A1 B1 A1✓	8	correct hypothesis - generous both hypotheses correct – requires population or μ 52.03(52~52.1) use of $\frac{8.5}{\sqrt{10}}$ correct method for z 4.10(4.10~4.11) 2.3263(2.32~2.33) – ignore sign conclusion in context AG – must be compared with upper tail of z
(a)(ii)	not a random sample – it contains only drivers prosecuted for speeding, who will be the fastest	E1 E1	2	not random reason

SS02 (cont)

Q	Solution	Marks	Total	Comments
(b)(i)	$H_0 : \mu = 30 \quad H_1 : \mu > 30$ $z = \frac{31.6-30}{\frac{6.9}{\sqrt{120}}} = 2.54$ c.v. = 1.6449 reject H_0 : significant evidence that mean speed exceeds 30 mph non-standardised c.v. $30 + 1.6449 \times \frac{6.9}{\sqrt{120}} = 31.04$ compare with 31.6 confidence interval $31.6 \pm 1.6449 \times \frac{6.9}{\sqrt{120}}$ 30.56~32.64 compare 30.56 with 30 p-value compare 0.00554 with 0.05	B1 M1 A1 B1 A1✓	5	both hypotheses method for z – ignore sign 2.54(2.53~2.55) 1.6449(1.64~1.65) – ignore sign ft conclusion in context – must be compared with upper tail of z
(b)(ii)	mean speed above 30 – indicates most cars probably above limit – although distribution probably skew so most may be below limit. since 31.6 significantly higher than 30 it will certainly be significantly lower than 41 so average speed has been reduced	E3,2,1	3	mean above limit/most speeding/ distribution skew/average speed reduced any sensible comments; E1 for each upto maximum 3
	Total		18	
	TOTAL		75	